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SEEFAR:

AN IMPROVED MODEL FOR PRODUCING LINE-OF-SIGHT
MAPS

NOV 31 1980

BARBARA D. BROOME

SEPTEMBER 1980

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20. ABSTRACT This report describes an improved model for producing line-of-sight maps. Many models determine whether a target is within view by drawing a terrain profile between observer and target and examining it to see if it interferes with line of sight; this requires generating a completely new profile for each target position. The new model avoids this time-consuming profile generation by dynamically recording the characteristics of a "running horizon" as computations are made for points further away from the observer. For each target point, a check is made to determine whether the target is behind the "horizon". This new approach results in a dramatic savings in both storage and computing time requirements.

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SEEFAR: AN IMPROVED MODEL FOR PRODUCING LINE-OF-SIGHT-MAPS

1. INTRODUCTION

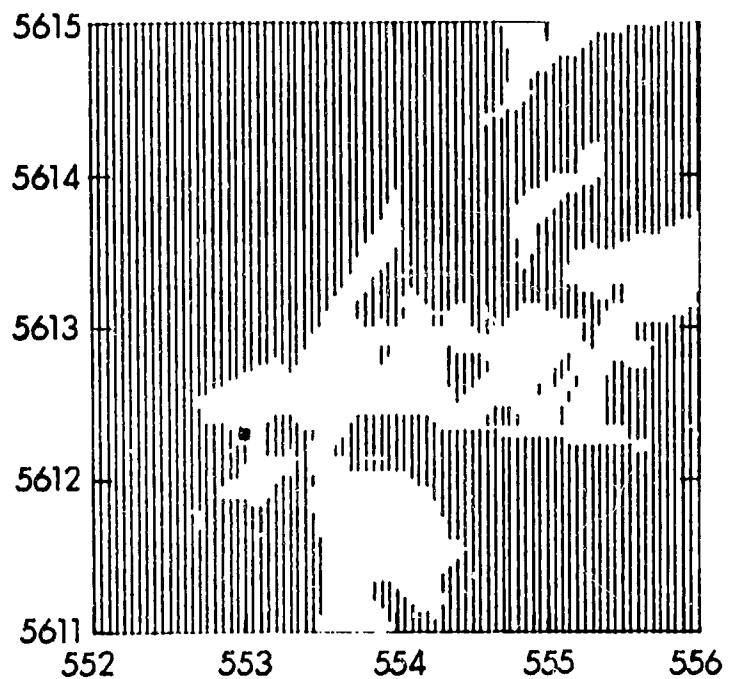
A line-of-sight map, or intervisibility plot, is a graphical representation of those portions of a geographical area which are visible to a given observer. (The term "visible" throughout this report refers to the existence of line of sight from an observation point to a target point which is uninterrupted by intervening terrain or obstacles.) These maps may be as shown in Figure 1, where the hatched portions represent those areas in which a target of a given height would be obscured. Targets in the blank portions would be visible. Or the maps may be shown as in Figure 2, where multiple target heights are considered. Each symbol plotted in a certain area indicates that targets of the associated height (or higher) located in this area are visible to the observer. For example, in Figure 2 a target 10 meters high (or higher) would be visible to the indicated observer if located at the point with UTM (Universal Transverse Mercator Projection) coordinates (554500, 5612600).

A number of computer programs are available for providing these maps; most of these programs are based on the algorithm described as "an intuitive approach" in this report. LOSMAP is one such program available at USAMSA. Use of an alternate algorithm, however, has resulted in a considerable reduction in both the memory requirements and compute time. An implementation of this algorithm, called SEEFAR, is included in Appendix A. The purpose of this report is to describe the basic SEEFAR algorithm and to compare it to the LOSMAP approach.

Line-of-sight maps have proved particularly useful in the development of combat scenarios for selecting reasonable observer positions and tactically sound attack routes. These maps can be useful to the wargamer, to the tactician in the field, and to the test plan developer. Additionally, they may be helpful in developing desirable weapon system characteristics. For example, it would be fruitless to develop a weapon system requiring line of sight with a range of 10 kilometers to be used in an area where observers typically cannot see a target at further than 5 kilometers.

The information required to produce these maps is of three types. First, the positional relationship between the map and observer must be specified. An area of interest is denoted by its extreme rectangular coordinates. The observer's position must be within this area. Secondly, heights of the observer and the target are required. The target height is the height of that point on the target that must be seen before the target is considered visible; the observer height designates the eye or sensor position above the ground. Finally, the actual terrain elevations along with any ancillary terrain data must be supplied.

The Defense Mapping Agency (DMA) digitized terrain data fulfill the third information requirement. These data were created by extracting elevations from contour lines on 1:50000 scale contour maps. Then, through planar interpolation, elevations were obtained at 12.5-meter intervals. This information

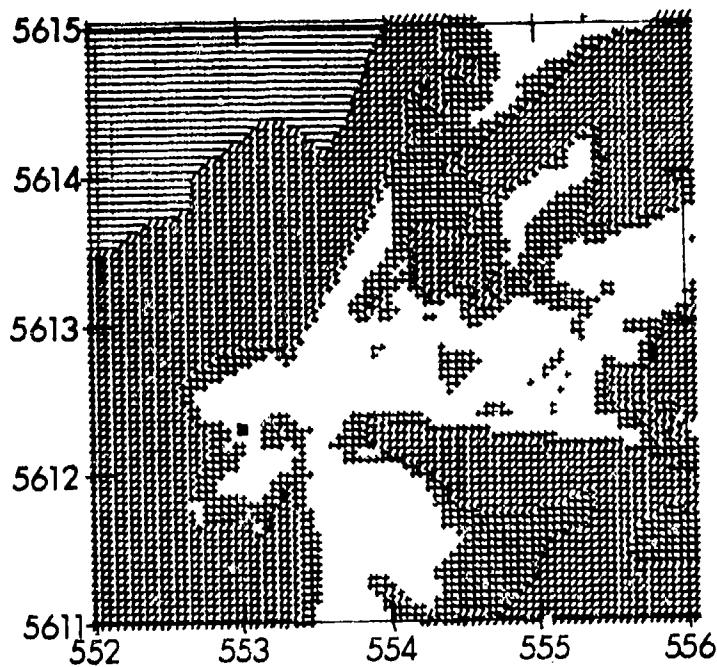


OBSERVER COORDINATES (553000 , 5612300)

OBSERVER HEIGHT = 2.00

OBSERVER ID = 1

Figure 1. Line-of-Sight Map.
Single Target Height



OBSERVER COORDINATES (553000, 5612300)

OBSERVER HEIGHT = 2.00

OBSERVER ID = 1

LEGEND

POSITION WHERE TARGET

X METERS HIGH OR MORE

CAN BE SEEN, WHERE

SYMBOL X =

2.00

+ 10.00

/ 100.00

- NO TARGET <= 100.00 METERS HIGH

CAN BE SEEN

Figure 2. Line-of-Sight Map
Multiple Target Height

is supplied on magnetic tapes as south-to-north strings of data sweeping from west to east. The term scanline, or scan, throughout this paper will denote a south-to-north string of information. Thus, the DMA data is a set of elevation scanlines. Additionally, an indication of the presence of a forest, orchard or urban area has been included with each elevation.

2. AN INTUITIVE LINE-OF-SIGHT ALGORITHM (LOSMAP)

2.1 Algorithm Description.

Now, given the information described in the previous section, suppose we wish to produce a map like that in Figure 1. Basically, at evenly spaced intervals throughout the area of interest the question must be asked, "Can the observer see the target if it is at this spot?" A reasonable approach to answering this question is to draw the terrain profile between the observer and the target, then draw the line from the observer eyeball to the target point and determine whether the terrain profile interrupts that observer-target line. If there is no interruption, line of sight exists; otherwise, this spot is not visible.

In Figure 3 the observer and target are depicted in the array of digitized elevations. As the figure indicates, at each point where the line between observer and target crosses a grid line, linear interpolation is used to find another height on the desired profile. As the profile is thus being constructed, a comparison is made between the elevation of each new point on the profile and the corresponding height of the line drawn from the observer eyeball to the target point. If the profile height is ever the larger of the two heights, line of sight does not exist; otherwise, line of sight does exit.

Of course this is a simplification of the problem. Because the presence of vegetation and urban areas can have a major impact on visibility for an observer, it is generally desirable to use the DMA vegetation/urban indicators. For example, while constructing the profile an appropriate height increment may be added to the profile if it runs through trees or towns. Further, the effect of earth curvature must be considered. If multiple target heights are considered, some accounting method must be used to keep track of the minimum visible target height. This brief description gives enough information to point out the major problems with the algorithm: computer space and time requirements.

2.2 Problems Encountered: Storage and Compute Time

As long as the area of interest is small, there is no problem. The use of high speed computers enables one to perform the required calculations with ease.

Notice, however, that this algorithm requires easy access to elevations in the entire area of interest. For each target point, an observer-to-target profile is constructed, requiring the elevations of many intervening points. Consider making a 6 x 6 kilometer map. If a 12.5-meter grid is used, an array of elevations dimensioned 481 x 481 is needed. Storing one elevation per word would require 231,361 words of memory for the elevation array alone! This problem can be somewhat alleviated by using a thinned grid of 25, 50 or even 100 meters. While this thinning may result in more inaccuracy, the outcome is often deemed adequate. Further, these elevations may be packed into the elevation array several at a time thereby decreasing the required storage even more. But, inevitably, as the size of the area that can be handled is increased, a problem is encountered that requires an area slightly larger. Some have solved the

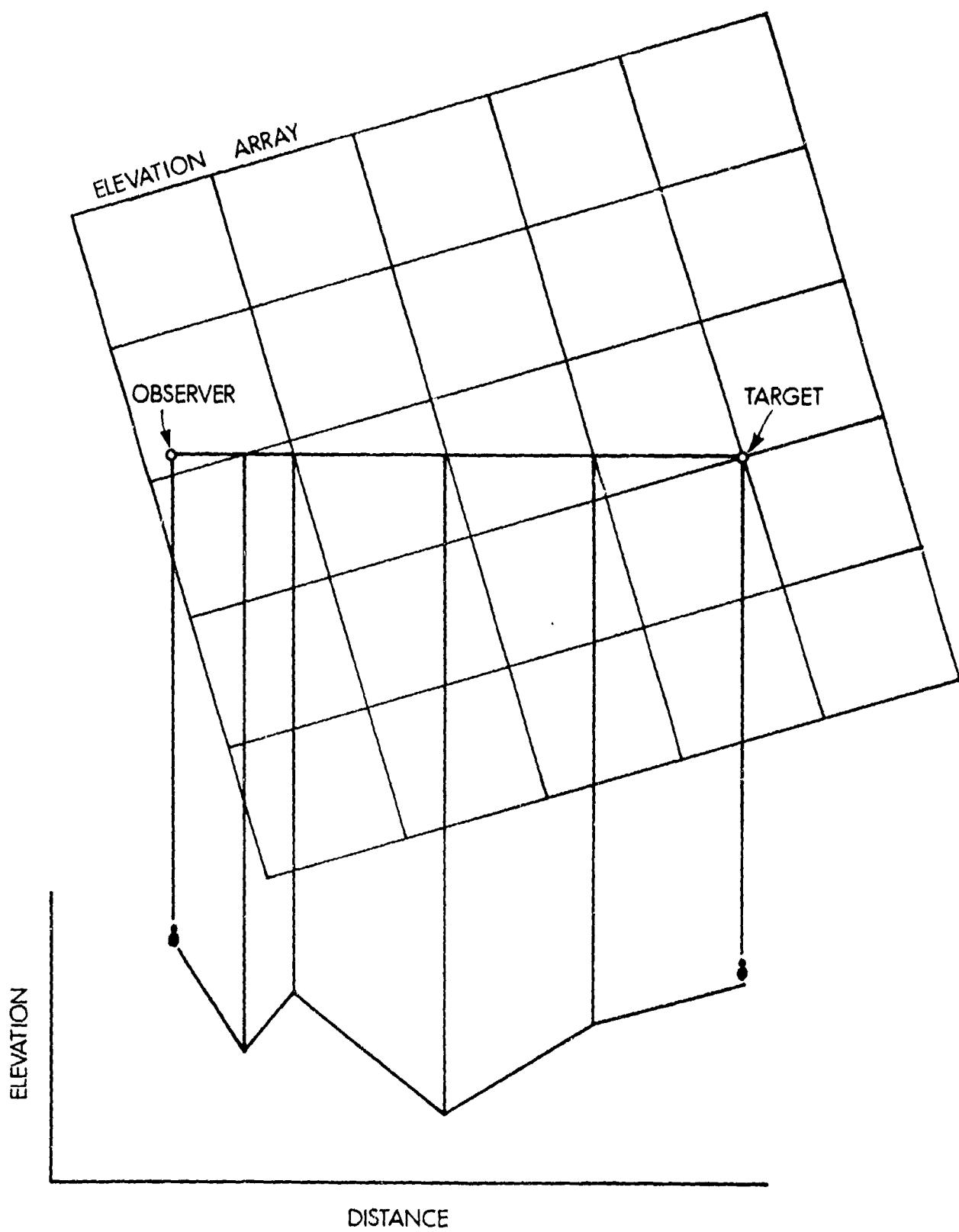


Figure 3. Constructing the Profile from Observer to Target.

storage problem by swapping data in and out of memory as needed. This, however, is rather cumbersome and will tremendously increase input-output time requirements. As one becomes concerned with larger areas of interest, as in air-to-ground and air-to-air intervisibility studies, this storage problem must be faced some other way.

Another problem to consider is that of compute time. If one needs a simple line-of-sight map like that in Figure 1, it is hard to predict exactly how many calculations will be performed. For each point on the map a profile must be started, so for an $n \times n$ map, at least n^2 calculations will be performed. If the profile interrupt is encountered early, few extra calculations will be needed. But, when line of sight to the target point exists, the entire profile must be constructed and each height comparison must be performed. With maps like that in Figure 2, considering multiple target heights, it becomes more likely that the entire profile must be constructed for every target point. The required number of calculations would then be of order n^3 (See Appendix C1). For large areas, this could easily be a prohibitively expensive algorithm.

3. DYNAMIC PROGRAMMING ALGORITHM (SEEFAR)

3.1 Algorithm Description.

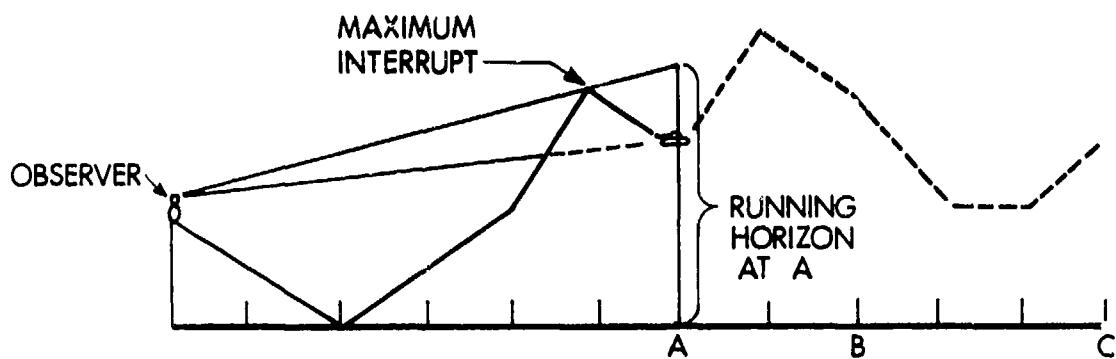
A. One Ray. Now consider an alternate approach to the development of line-of-sight maps. How should line-of-sight calculations be performed if all the target positions lay along one line? For each target position along the ray the question must be answered, "How high must the target be raised to be seen?" But it hardly seems necessary to draw a new profile for each target position. Instead, one might choose to work from the observer out, extending the profile to each new target position, not keeping track of all the previously encountered elevations but simply updating the effect of the maximum interrupt encountered thus far as new interrupts are encountered. This maximum interrupt effect projected to the current target position is essentially the minimum target height required to overcome the effect of terrain between the observer and the target. This height can be thought of as a running horizon, running in the sense that it must be updated as target positions move further from the observer.

For each target position, then, the following procedure could be followed:

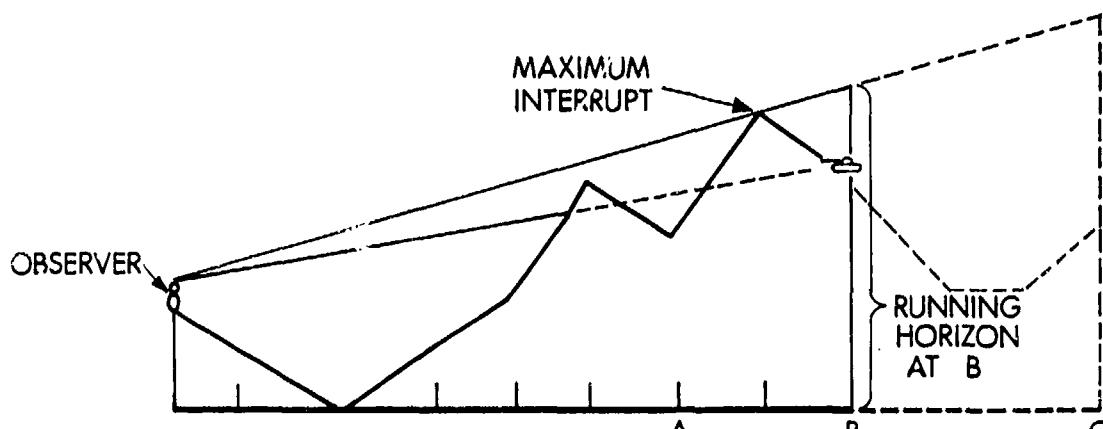
- (1) Check to see if the current target position is above or below the current horizon (i.e., in or out of view)
- (2) Plot the results
- (3) Update the running horizon to reflect its movement outward, and any greater interrupts encountered. (This new horizon value will be used in the line of sight calculation for the next target position.)

Consider now this running horizon, or maximum interrupt effect. Figure 4 demonstrates maximum interrupts, how they can change as the profile is extended, and how their corresponding projected effect must continually be updated. The maximum interrupt effect must be updated both as new interrupts are encountered and as the target position is changed. A comparison of Figures 4A and 4B demonstrates the need to update the running horizon as greater interrupts are encountered. Considering Figures 4B and 4C, it can be seen that the effect of the maximum interrupt will vary for different target positions even though the maximum itself may remain the same. One should further note that, as shown in Figure 5, the maximum interrupt is not necessarily the terrain profile with the highest elevation.

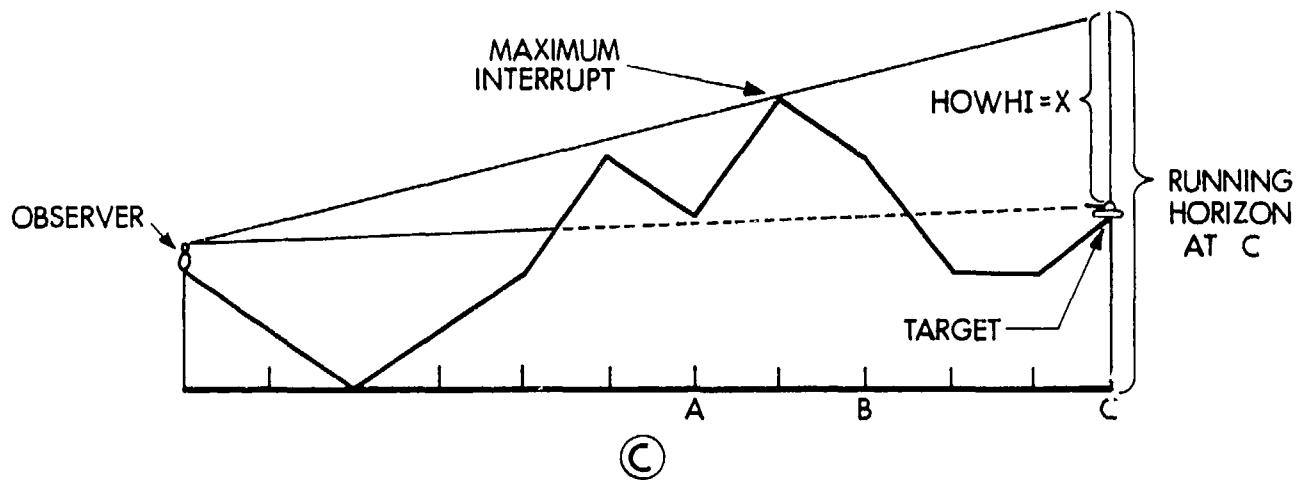
This procedure has several nice features. First, because it is not necessary to draw a new profile for each target position, fewer steps are required. Further, it is not necessary to store all the elevations between the observer and the target to determine whether line of sight exists. The elevation of the current target position and the horizon effect are the only values needed. This method can be extended to produce a full map, rather than a single ray, greatly reducing the storage and compute time problems.



(A)



(B)



(C)

Figure 4. Updating the Running Horizon (The Effect of the Maximum Interrupt Projected to the Target Position)

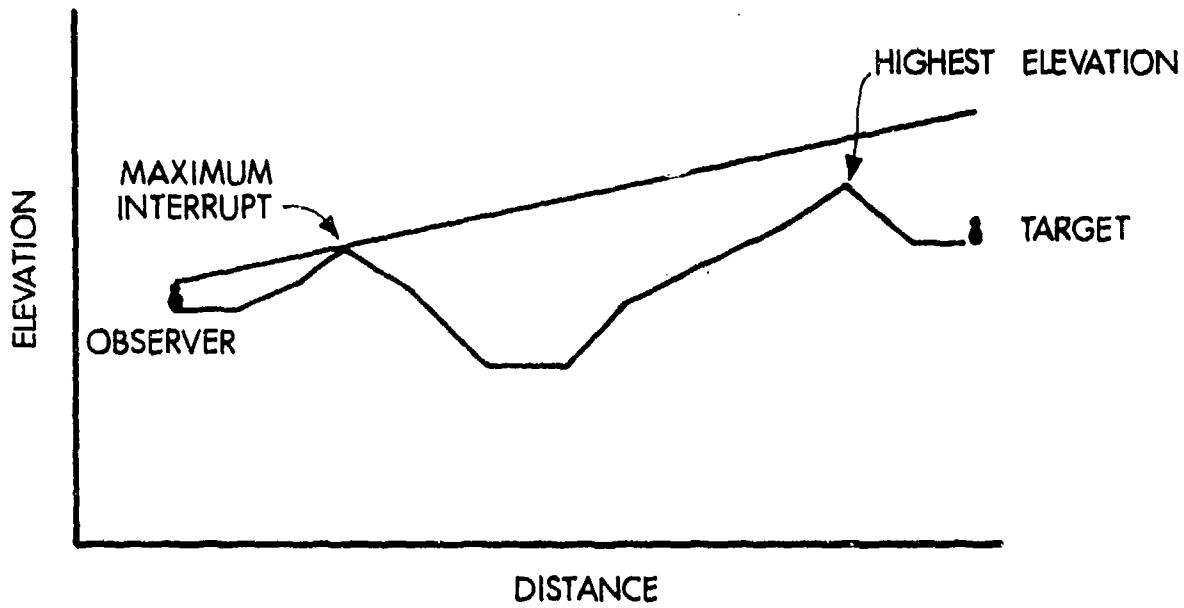


Figure 5. Maximum Interrupt Not Always Highest Elevation.

B. Full Map.

(1) Radial Map. Now how can this one-dimensional algorithm be expanded to two dimensions? One approach would be to produce a radial line-of-sight map, extending many profiles out from the observer. Certainly if line-of-sight information can be produced for one ray as described in the previous section, it would be a simple matter to project rays from the observer at small equally-space angle increments, combine the results and produce a two-dimensional map. With this method, however, the line-of-sight information would be very closely spaced near the observer and more widely spaced farther from the observer. As the profiles got further apart the likelihood of missing an important terrain feature would increase. Assuming, then, that evenly spaced data is more desirable, another method must be devised to produce the two-dimensional maps.

(2) Rectangular Map. As in the ray method the approach will be to work from the observer out (i.e., from the observer eastward, then from the observer westward), keeping track of a running horizon. But this time instead of having a running horizon point, there will be a south-to-north string of running horizon points (a horizon scanline) sweeping outward from the observer as the calculations are performed.

Remember, the map is actually a lattice of target spots. The goal is to determine for each target spot the value that denotes how high a target must be to be seen. Let $HOWHI(i)$ be the height the i th target must be raised to be seen. If the target height is less than $HOWHI(i)$ it cannot be seen; otherwise it can. The following sections describe a method for obtaining $HOWHI(i)$'s. In order to reach this goal one must continually keep up with $HORIZON(i)$, the effect of the maximum interrupt encountered between the observer and the current target position.

Scans Closest to Observer

Because the plan is to work outward from the observer, the first step is to perform calculations for the two target scanlines closest to the observer. In checking for line of sight to the points on these scans, the first iterations of the east-running horizon and west-running horizon must also be formed. Figure 6 will help illustrate this procedure.

Consider the point 1R (as in Figure 6A). First determine how high a target must be to be seen at position 1R. There are obviously no terrain profile elevations between the observer and this point, so one might automatically say $\text{HOWHI}(1R) = 0$. But if forests and urban areas are to be considered a check must be made to determine whether such an obstacle is located at 1R. If so, $\text{HOWHI}(1R) = 0 + \text{HVEG}(1R)$ where HVEG is the height of the obstacle. If the target height is less than $\text{HOWHI}(1R)$, a target at 1R cannot be seen and the appropriate symbol must be plotted. But more must be done at this position. The running horizon value at 1R must be determined. The highest elevation (vegetation and urban included) encountered between the observer and 1R is simply the elevation at 1R (there are no elevations given elsewhere) plus the obstacle height at 1R. Thus, $\text{HORIZON}(1R) = E(1R) + \text{HVEG}(1R)$ where $E(1R)$ is the terrain elevation at 1R. A similar procedure for position 1L results in $\text{HOWHI}(1L) = 0 + \text{HVEG}(1L)$ and $\text{HORIZON}(1L) = E(1L) + \text{HVEG}(1L)$.

Now consider the point 2R (as in Figure 6B). Determine the maximum elevation encountered between the observer and position 2R. This is the horizon value at (X, Y) , i.e., Z, where Z is the linear interpolation between the horizon at 1L and the horizon at 1R (See Appendix B1 for a discussion of the calculation of X, Y, & Z). Now project this Z value to the position 2R, obtaining $Z'(2R)$ (as described in Appendix B2). In order to be seen, the target point must be higher than $Z'(2R)$, so $\text{HOWHI}(2R) = Z'(2R) - E(2R)$. In addition the vegetation must be considered. To guarantee the target is above the ground $\text{HOWHI}(2R)$ must be the maximum of either $\text{HVEG}(2R)$ or $Z'(2R) - E(2R)$. Once HOWHI is determined the proper symbol is plotted for this point. Now the horizon at 2R must be computed. The horizon will simply be the maximum of (the projection of the old horizon to 2R) and (the current elevation, vegetation/urban included).

That is, $\text{HORIZON}(2R) = \text{MAX}(Z'(2R), E(2R) + \text{HVEG}(2R))$

Similarly, $\text{HOWHI}(2L) = \text{MAX}(Z'(2L) - E(2L), \text{HVEG}(2L))$

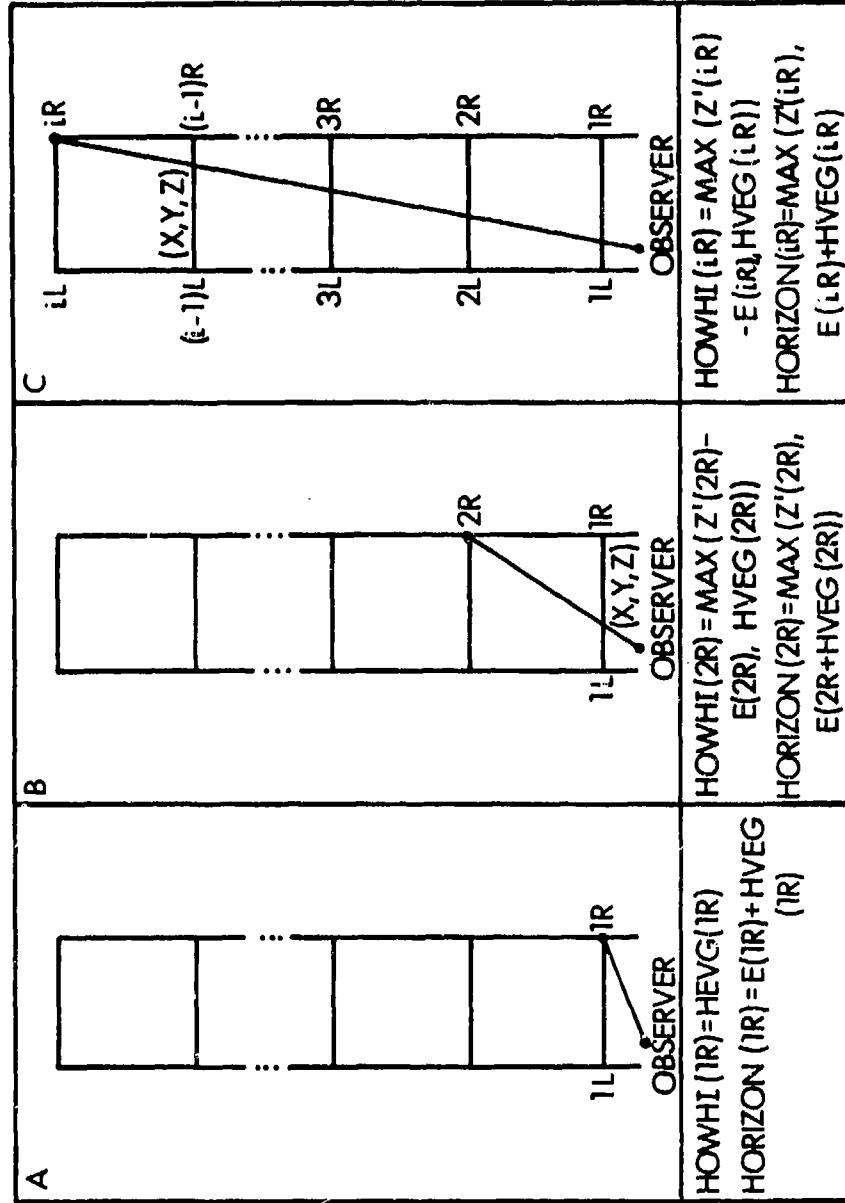
and $\text{HORIZON}(2L) = \text{MAX}(Z'(2L), E(2L) + \text{HVEG}(2L))$.

In general, for the i th point above the observer (See Figure 6C)

$\text{HOWHI}(i) = \text{MAX}(Z'(i) - E(i), \text{HVEG}(i))$

and $\text{HORIZON}(i) = \text{MAX}(Z'(i), E(i) + \text{HVEG}(i))$.

Points south of the observer should be handled in a manner similar to those north of the observer, resulting in identical equations for $\text{HOWHI}(i)$ and $\text{HORIZON}(i)$.



- = TARGET POSITION

iL = i th POSITION ON LEFT SCAN
 iR = i th POSITION ON RIGHT SCAN
 $E(iL)$ = DMA ELEVATION AT iL
 $Z'(iL)$ = PROJECTION OF Z TO TARGET POSITION iL
 $\text{HVEG}(iL)$ = VEGETATION/URBAN HEIGHT AT iL

Figure 6. Calculation of HOWHI and HORIZON for Scans Closest to the Observer.

Scans East of Observer

Consider scanline R_2 in Figure 7A, consisting of points $(...OR_2, 1R_2, 2R_2, 3R_2, \dots(n=1)R_2, nR_2)$. In order to obtain HOWHI's for this line, only the horizon values for scanline R and the terrain elevations for Scanline R_2 are needed. Working upward from the observer, the first target point to consider is $1R_2$. Check the terrain elevation at $1R_2$. This must be compared with the effect of the maximum interrupt encountered earlier (the horizon effect). The intersection of the observer-target line with the line of known horizon values closest to the target is at (X,Y) . A linear interpolation between $HORIZON(1R)$ and $HORIZON(OR)$ will provide Z, the horizon height at (X,Y) . Project Z to $1R_2$, obtaining $Z'(1R_2)$. Then

$$HOWHI(1R_2) = \text{MAX}(Z'(1R_2) - E(1R_2), HVEG(1R_2))$$

and $HORIZON(1R_2) = \text{MAX}(Z'(1R_2), E(1R_2) + HVEG(1R_2))$.

Similarly, using Figure 7B, the appropriate values for point $2R_2$ can be determined.

Figure 7C depicts a variation in this method. The observer-target line intersection with the line of known horizon values closest to the target is not along line R, but rather at a point (X,Y) between target points $2R$ and $2R_2$. In this case the HOWHI and HORIZON equations are as follows:

$$HOWHI(3R_2) = \text{MAX}(Z'(3R_2) - E(3R_2), HVEG(3R_2))$$

$$HORIZON(3R_2) = \text{MAX}(Z'(3R_2) + E(3R_2) + HVEG(3R_2))$$

Thus the intersection of the observer-target line with the closest vertical horizon scan line is not necessarily the intersection of interest. The explanation in Appendix B1 for deriving X, Y and Z takes both of the cases into account.

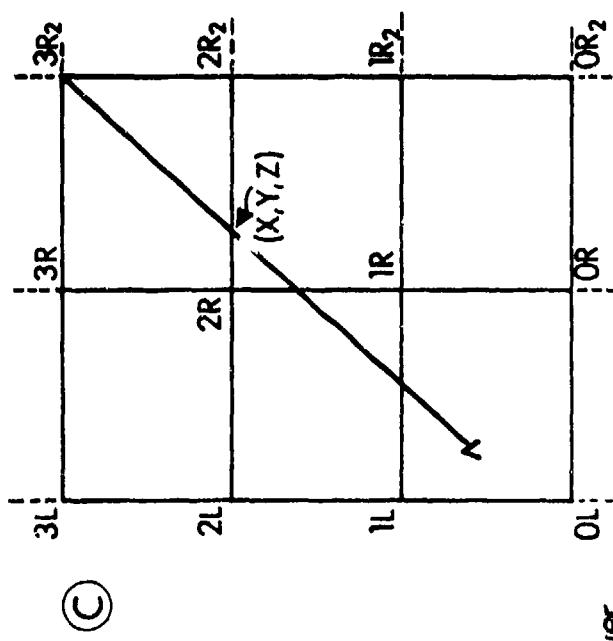
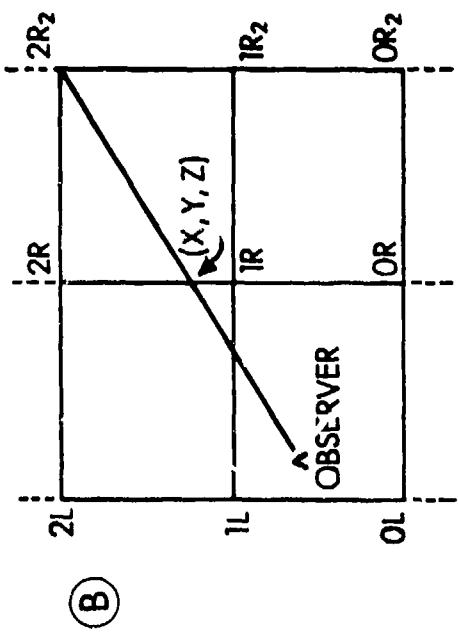
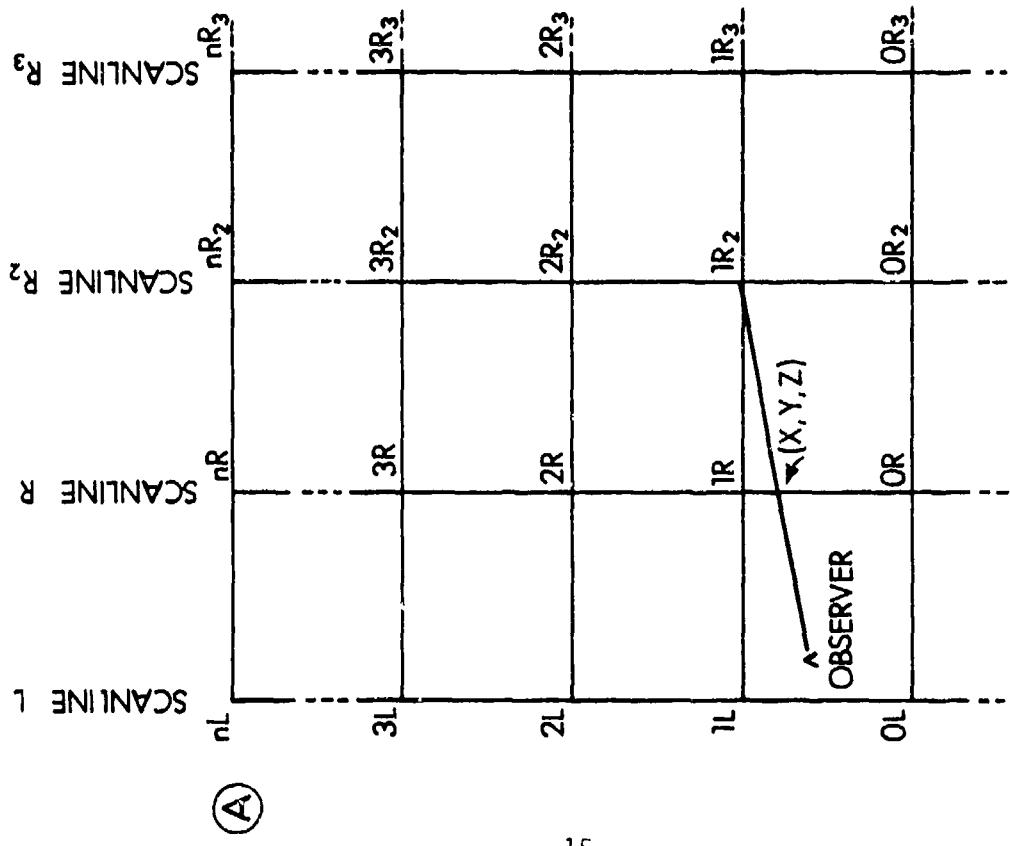


Figure 7. Calculations for Scans East of the Observer.

Scans West of Observer

In general, for points east of the observer

$$\text{HOWHI}(i) = \text{MAX } (Z'(i) - E(i), \text{HVEG}(i))$$

$$\text{HORIZON}(i) = \text{MAX } (Z'(i), E(i) + \text{HVEG}(i))$$

By simply reversing directions and starting with the horizon values corresponding to scanline L (calculated while working with scans closest to the observer) the same equations are found to apply to points west of the observer. Variations in the computation of values (X,Y,Z) in determining horizon effects are all accounted for in Appendix B1.

Algorithm Outline

In short, the map can be thought of as a lattice of equally spaced target positions. These are the points for which terrain elevations are available and can be thought of as south-to-north strings of target positions, or target scanlines. The following provides a general outline of the flow of the algorithm:

FIND AND PLOT LINE OF SIGHT INFORMATION FOR SCANS CLOSEST TO OBSERVER, WHILE CREATING ORIGINAL HORIZONS EAST AND WEST OF OBSERVER.

FOR SCANS FROM OBSERVER TO SIDE BOUNDARY (FIRST EASTWARD THEN WESTWARD DO:

READ ELEVATIONS FOR SCAN OF INTEREST

FOR POINTS FROM OBSERVER NORTH THEN FROM OBSERVER SOUTH DO:

FIND INTERSECTION OF OBSERVER-TARGET LINE WITH HORIZON LINE CLOSEST TO TARGET

INTERPOLATE BETWEEN KNOWN HORIZON VALUES TO OBTAIN HORIZON VALUE

PROJECT HORIZON VALUE TO CURRENT TARGET POSITION (TAKING INTO ACCOUNT THE EFFECT OF EARTH CURVATURE)

COMPARE CURRENT ELEVATION WITH PROJECTED HORIZON TO DETERMINE WHETHER LINE OF SIGHT EXISTS

UPDATE HORIZON VALUE

PLOT RESULTS

STOP

3.2 Solution to Storage and Compute Time Problem.

A. Storage. The savings in storage requirements for the SEE-FAR algorithm are considerable. The profile algorithm required all the elevation data to be easily accessible, since many scans of data were needed to produce each profile; the newer algorithm needs only the current scanline of elevation data and the most recently updated horizon information to perform the necessary computations. The amount of random access memory required, then, is a function of the north-to-south dimension of the map rather than the area of the map. A map that is 100 x 50 kilometers in size would take no more main memory than a map 1 x 50 kilometers, given equal grid size. The original algorithm would have taken 100 times more storage. Maps that would have been virtually impossible with the old algorithm are now quite possible. But if only storage requirements are reduced, the reader may wonder whether the machine time requirements would be prohibitive for production of these larger maps. The savings in computing time resulting from this approach must be considered.

B. Computing Time. As mentioned earlier, the original algorithm required on the order of n^3 operations for an $n \times n$ sized map, because each profile consists of many points, and each of these points might have to be considered in a single line-of-sight calculation. The newer algorithm, however, simply compares the current target elevation with the horizon effect at the target point. Thus, a small fixed number of calculations are required for each target point on the map. This algorithm is, then, of the order n^2 for an $n \times n$ map. For maps of larger sizes the computing time savings will be considerable. It can in many instances be the difference between a map reasonably produced and one so expensive in computation cost that its value to the tactician or analyst cannot outweigh the expense. Note that since n^2 target points are involved in an $n \times n$ map, order n^2 is the minimum possible complexity. A few examples of these differences are discussed in the following section.

4. COMPARISON OF MAPS RESULTING FROM EACH ALGORITHM

4.1 Discussion. The LOSMAP and SEE FAR algorithms discussed are quite different in nature. While each uses a method of linear interpolation to get results, the intuitive method interpolates between known elevations to get elevations along a profile, then checks to see if those elevations interrupt line of sight. The dynamic programming approach, on the other hand, keeps up with the effect of maximum interrupts encountered via the horizon array. A linear interpolation is made between horizon values to find a projection of the horizon to a specific target point. It is not surprising to discover the results of these methods are not always the same. But, while the "intuitive" LOSMAP method described uses interpolation and is therefore not an exact solution to the line of sight problem, it would be disappointing to find large discrepancies in the results of the two approaches. One would certainly hope the results of a new approach would conform somewhat to those of an intuitive method.

As it turns out, the results are quite similar. In fact, very close inspection is generally required to distinguish differences in line-of-sight maps with one target height. It is easier to detect differences when multiple target heights are used. The SEE FAR approach might at one time indicate a target visible that the LOSMAP approach indicated nonvisible. Another time the reverse situation might occur. In general, however, the boundaries of in-view and out-of-view areas do not differ widely between algorithms. It should be added that, while the dynamic programming approach may not be the first to come to mind when tackling the line-of-sight problem, it is a reasonable approach, one certainly not counter to intuition. And the savings in time and storage cannot be ignored.

4.2 Sample Maps. The following pages will provide the reader an opportunity to compare the results of the two algorithms.

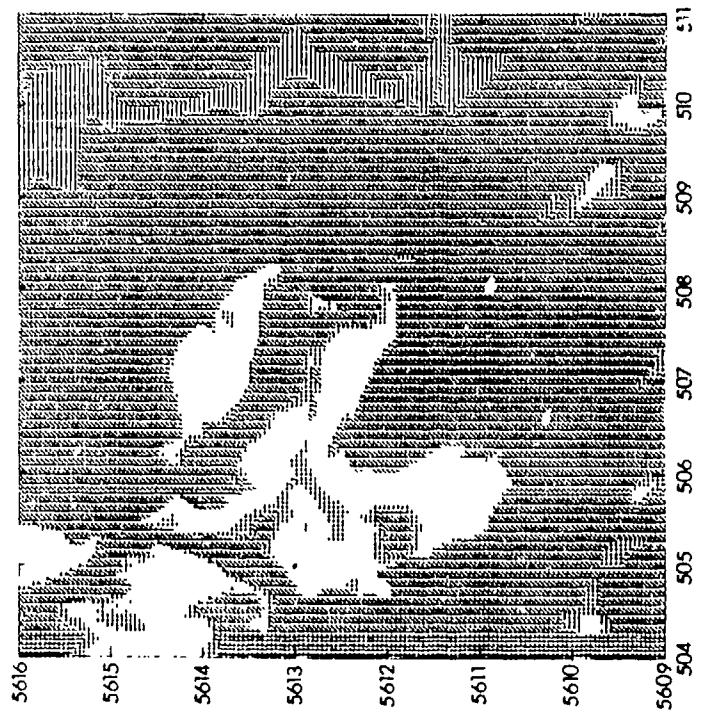


Figure 8A. LOSMAP Algorithm.
Compute Time : 166 Sec.

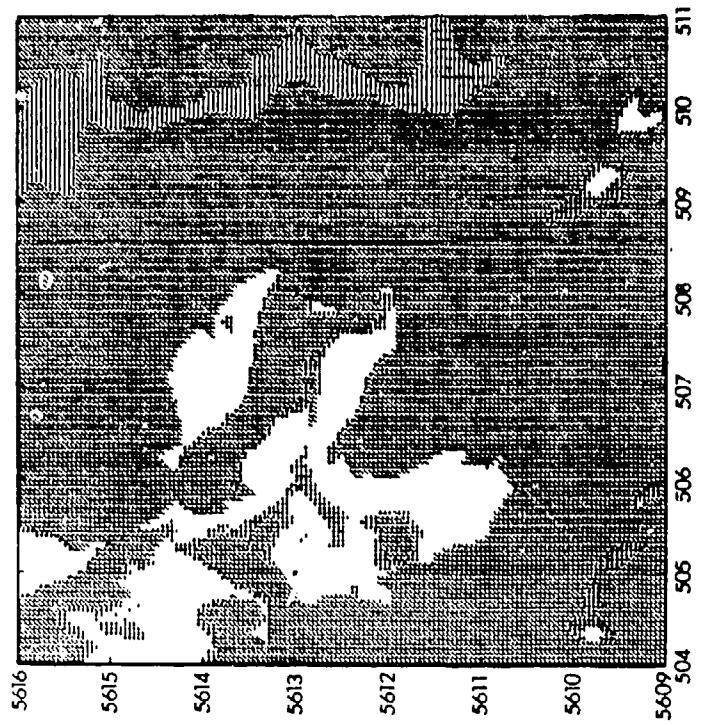


Figure 8B. SEE FAR Algorithm.
Compute Time : 17 Sec.

Figure 8B. SEE FAR Algorithm
Compute Time : 17 Sec.

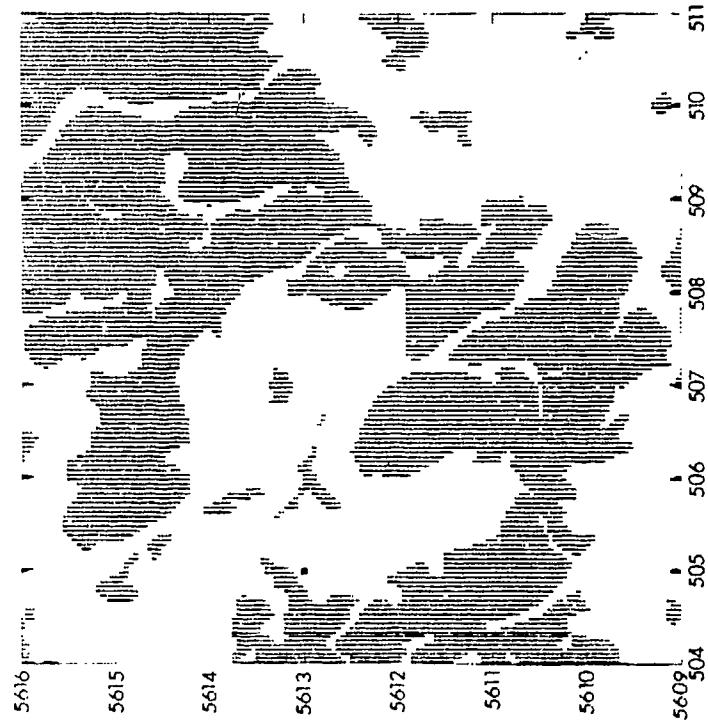


Figure 9A. LOSMAP Algorithm.
Compute Time: 162 Sec.

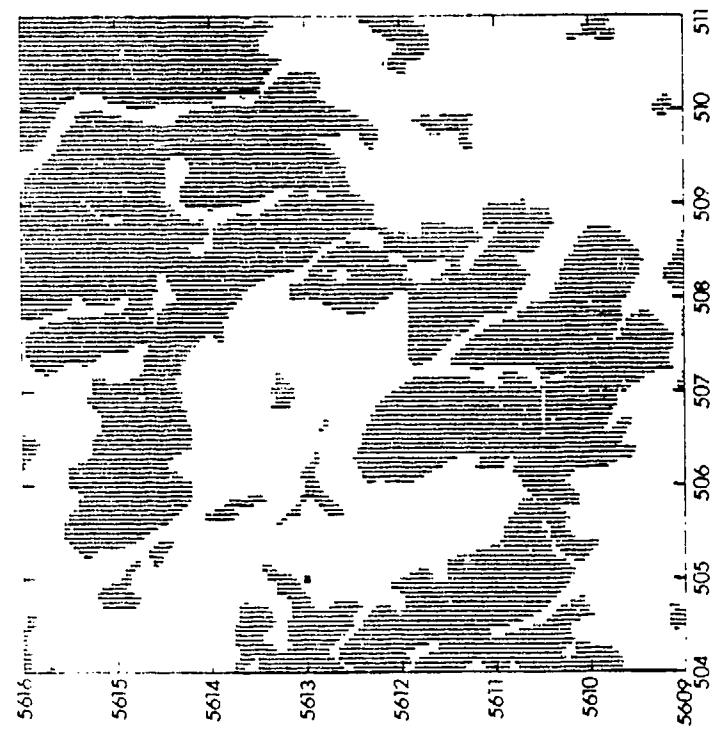
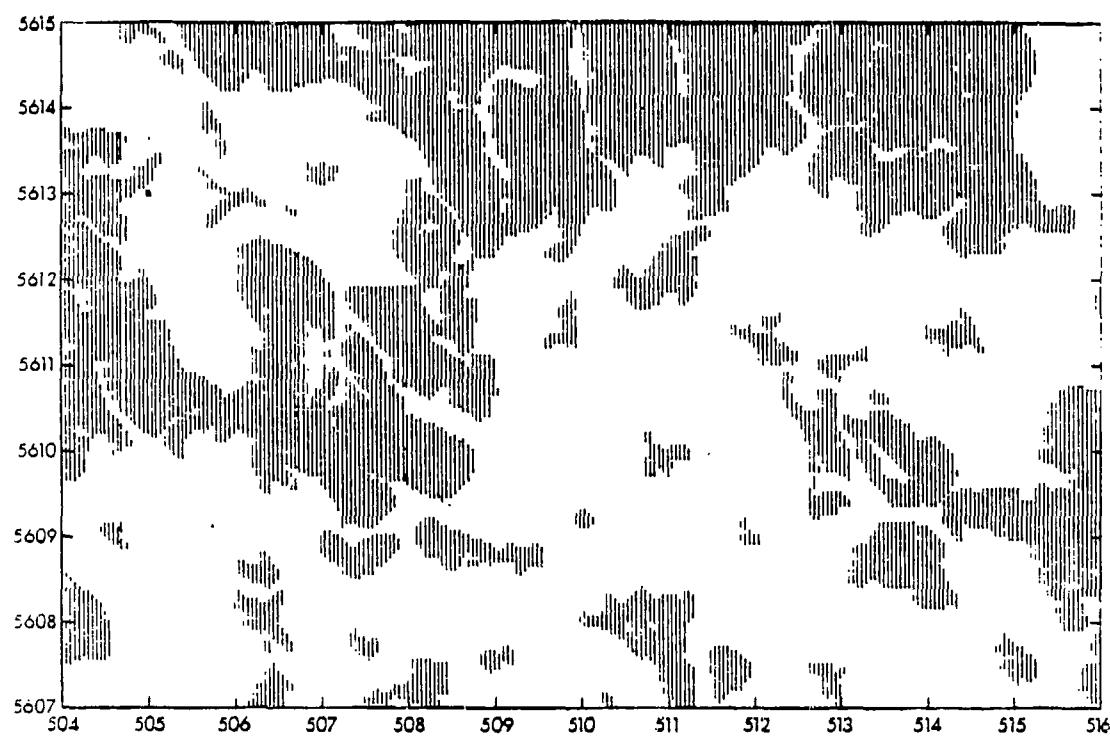
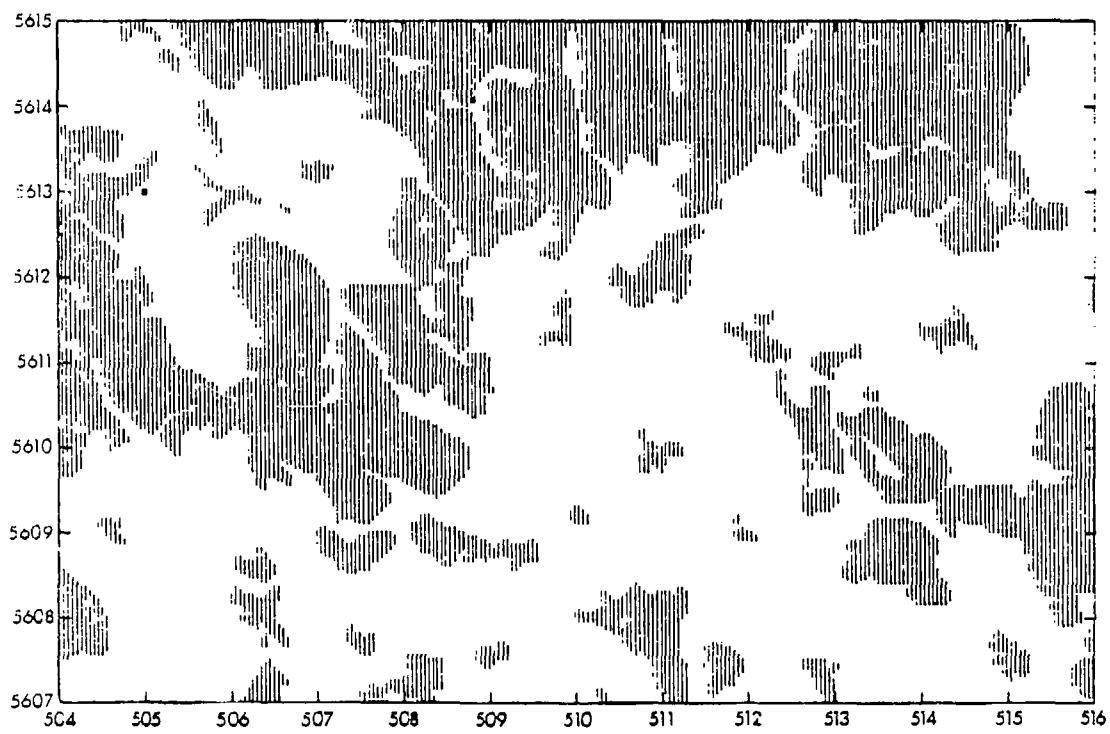


Figure 9B. SEEFAIR Algorithm.
Compute Time: 14 Sec.



MAP OF POINTS VISIBLE TO A SINGLE OBSERVER
 OBSERVER COORDINATES (505000, 5613000)
 OBSERV. HEIGHT = 2000.00
 TARG. HEIGHT = 1.50

Figure 10A. LOSMAP Algorithm
 Compute Time: 576 Sec.



OBSERVER COORDINATES (505000, 5613000)
 OBSERVER HEIGHT = 2000.00
 OBSERVER ID = 1

Figure 10B. SEE FAR Algorithm
 Compute Time: 20 Sec.

5. SUMMARY

5.1 Advantages of the SEE FAR Algorithm. The SEE FAR algorithm, then, provides a method for generating line-of-sight maps (and thereby obtaining intervisibility data) for a much larger area or for a smaller grid than could reasonably be provided using the LOSMAP algorithm. This dynamic programming approach results in an order of complexity of n^2 for an $n \times n$ map, which is the minimum that can be expected. Further, it reduces the storage requirements such that only one scanline of elevation data need be in memory at any one time. Thus, it is an order of magnitude better than the LOSMAP algorithm in both time and storage requirements.

5.2 The SEE FAR Program. Appendix A1 contains a copy of the SEE FAR program, an implementation of the algorithm discussed in this report. It should be noted that the algorithm discussion is concerned with the basic approach to the line-of-sight problem. The SEE FAR program has several embellishments. First, if an observer is in a forest/urban area, and the proper option is selected, SEE FAR will attempt to move the observer out of the obstruction. Second, the ratio of visible-to-total targets in a selected area of interest is given. Third, terrain data on as many as 12 DMA tapes can be merged and put into a direct access file. Finally, the HOWHI array, which indicates for every target position how high the target must be raised to be seen by the selected observer, can be saved on a permanent file. This allows one, through short fast-running programs, to vary target heights or merge line of sight data for several observers obtaining maps which indicate areas visible to m-out-of-n observers ($1 \leq m \leq n$). These m-out-of-n maps, or composite maps, are done by a separate program now, but could easily be provided via the SEE FAR program.

5.3 Problems Remaining. There are line-of-sight data requirements for which SEE FAR does not seem a viable alternative. For example, the LOSPATH program, in use at AMSAA, checks along paths for line of sight. To use SEE FAR for this problem one must generate a rectangular map containing all the path points and then check for line of sight at appropriate points within the rectangle. Because SEE FAR builds on information generated for all the points between the observer and the current target position, it does not seem optimal when target points are in scattered positions rather than at evenly spaced intervals within a rectangle of interest.

The question of how much discrepancy to expect between the LOSMAP and SEE FAR algorithms has not been determined analytically. This may be of interest; but since each approach provides an interpolated approximation to the line-of-sight problem, the value of such an analysis is questionable.

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Virbila, J.P., MASKPAS PROGRAMS Digitized Terrain, Flight Path Generator, Intervisibility for Evaluation of Air Defense Effectiveness, Vol 1, Joint Technical Coordinating Group for Munitions Effectiveness, U.S. Army Materiel Systems Analysis Activity, Aberdeen Proving Ground, MD.

APPENDIX A

SEEFAR USER'S AIDS

A-1

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APPENDIX A1

SEEFAR PROGRAM

```

PROGRAM SEEFAR(INPUT, OUTPUT, TAPE5=INPUT, TAPE6=OUTPUT,
*           TAPE7, TAPE8, TAPE9, TAPE10, TAPE11, TAPE12,
*           TAPE14, TAPE15, TAPE16, TAPE17, TAPE18, TAPE19,
*           TAPE2, TAPE3,
*           TAPE13)

C ***
C BY BARBARA BROOME
C PRODUCES LINE OF SIGHT MAP USING DYNAMIC PROGRAMMING ALGORITHM.
C LOS DATA (THE IOWHIS ARRAY) CAN BE STORED ON DISK FOR LATER WORK.
C CALCULATES FRACTION OF (VISIBLE AREA) / (NON-VISIBLE AREA) FOR
C DISTANCE OF INTEREST.
C TAPE13 HOLDS PLOT DATA
C TAPE2 HOLDS MERGED TERRAIN DATA
C TAPE3 HOLDS IOWHI DATA FOR FUTURE MAPS
C TAPE5 HOLDS CARD INPUT
C TAPE6 HOLDS PRINTED OUTPUT
C ALL OTHERS ARE DNA TERRAIN DATA TAPE8 (PRE-MERGE)

C ***
C COMMON STATEMENTS
COMMON /SE/ XOBG, YOBG, HOBG, OBTRAN
COMMON /AF/ XORIGN, YORIGN, XSTOP, YSTOP
COMMON /SCANS/ NM, NY
COMMON /PLTSTR/ NMID, SCALC, NPLHT, PLHT(10), ICDS, INK
COMMON /BIG/ HOWHI(4000)
COMMON /ASHSTF/ RNUM(20), DNUM
COMMON /BOX/ BOMMIN, BOXMAX, BOYMIN, BOYMAX, IBOX
COMMON /OTHER/ IDNTWV, ITOTAV, YMIN, XMAX, YMINS, YMAX, NTAPES,
*                 TGIRD, ISAVE
COMMON /VEGIND/ JVEG
REAL L1OWHI(4000)
COMMON /ZS/ ZOLD(4000), ZNOW(4000), ZLATER(4000)
CALL EDNCHK

C ***
C PUT DNA ELEVATIONS INTO DIRECT ACCESS FILE (UNIT 2).
C MODIFY BOUNDARY COORDINATES TO CORRESPOND WITH DNA COORDINATES.
C *EXPOSE OBSERVER AND FIND OBS. ELEVATION (HUBS NOT INCLUDED)
C ***
CALL MERGIT(NTAPES, TGIRD, GRIDE, XIIM, XMAX, YMINS, YMAX,
*                 NY, NY, XORIGN, YSTOP, XSTOP, YSTOP)
CALL XPOSIT(XOBG, YOBG, IDNTWV)
OBTRAN = ELVIND(XOBG, YOBG, XORIGN, YSTOP, GRIDE)
WEITL(6, 950) OBTRAN

C ***
C PLOT PRELIMINARY INFO. (AMOC, OBSERVER COORDINATES, ETC).
C PLOT LOS INFO FOR SCANS CLOSEST TO OBSERVER
C SAVE ZOLD IN LHOWHI - USE IT AS 1ST ZOLD FOR SCANS WEST OF OBS.
C SAVE ZLATER - USE IT AS 1ST ZOLD FOR SCANS EAST OF OBS.
C IF SAVING MAP ON DISK, PUT PRELIM. INFO. IN REC 4001-4013 & SAVE
C ***
XTOT = INT((XOBG-XORIGN+.00001)/GRIDE) * GRIDE + XORIGN + GRIDE
CALL FLTPRE(XIIM, XMAX, YMINS, YMAX)
IF (ISAVE .EQ. 1) CALL SAVPRE(1,XTOTAV)
CALL FSTCH(EXTOT, LHOWHI, HOWHI, ZCOL1)
CALL PLTLN(LHOWHI, ZCOL1-1, XTOTAV)
CALL PLTLN(HOWHI, ZCOL1, XTOTAV)
IF (ISAVE .EQ. 1) CALL WRITREC(3,LHOWHI(1), NY, ZCOL1-1)

```

```

IF (ISAVE .EQ. 1) CALL WRITMS(3, HOWHI(1), NY, ICOL1)
DO 200 I = 1, NY
  LHOWHI(I) = ZOLD(I)
CONTINUE
200
C ***
C   FILL HOWHI & PLOT FOR EACH LINE EAST OF OBSERVER
C ***
ICOL2 = ICOL1 + 1
IF (ICOL2 .LT. NX) GO TO 450
DO 400 ICOL = ICOL2, NX
  DO 300 I = 1, NY
    ZOLD(I) = ZLATER(I)
300
CONTINUE
CALL READMS(2, ZHOW(1), NY, ICOL)
CALL ONELN(ICOL, HOWHI)
CALL PLTLN(HOWHI, ICOL, ITGTAV)
IF (ISAVE .EQ. 1) CALL WRITMS(3, HOWHI(1), NY, ICOL)
400
CONTINUE
450 CONTINUE
C ***
C   FILL HOWHI & PLOT FOR EACH LINE WEST OF OBSERVER
C ***
ICOLM2 = ICOL1 - 2
IF (ICOLM2 .LT. 1) GO TO 800
ICOL = ICOL1 - 1
DO 500 I = 1, NY
  ZLATER(I) = LHOWHI(I)
500
CONTINUE
DO 700 I = 1, ICOLM2
  ICOL = ICOL - 1
  DO 600 J = 1, NY
    ZOLD(J) = ZLATER(J)
600
CONTINUE
CALL READMS(2, ZHOW(1), NY, ICOL)
CALL ONELN(ICOL, HOWHI)
CALL PLTLN(HOWHI, ICOL, ITGTAV)
IF (ISAVE .EQ. 1) CALL WRITMS(3, HOWHI(1), NY, ICOL)
700
CONTINUE
800 CONTINUE
IF (IDBX .NE. 0) CALL PRFRON
CALL PLTPGE
STOP
C ***
C   FORMATS
C ***
950 FORMAT(' ELEVATION OF TERRAIN AT OBSERVER POSITION =', F10.1)
END

```

```
SUBROUTINE DCDMAX ( X, Y, NREC)
C ***
C BY MONTE COLEMAN
C RETURNS X AND Y COORDINATES FROM DATA RECORD ALONG WITH RECORD NO.
C ***
C COMMON /DMACOM/ IBUF(700), ITEMP(80), ITEM
C DATA XSCALE/ 1.00 /, YSCALE / 1.00 /
C
C CALL UNPACK (IBUF, ITEMP, 10)
NREC=ICVT(ITEMP(4), 3)
X=FLOAT(ICVT(ITEMP(7),2))*XSCALE
Y=FLOAT(ICVT(ITEMP(9),2))*YSCALE
RETURN
END
```

```
SUBROUTINE DCTID (ISH, ISER, IED, XCOR, YCOR)
C *** BY MONTE COLEMAN
C DECODES A TAPE ID BLOCK
C ISH = MAP SHEET IDENTIFICATION
C ISER = MAP SERIES IDENTIFICATION
C IED = MAP EDITION IDENTIFICATION
C CORNERS IN ORDER SW, NW, NE, SE
C ***
COMMON /DMACOM/ IBUF(700), ITEMP(80), ITEM
DIMENSION XCOR(4), YCOR(4), ISH(2)
CALL UNPACK (IBUF, ITEMP, 70)
CALL FDTATE (ITEMP(7), 12)
CALL PACK (ITEMP(7), ISH, 12)
ISER=ICVT(ITEMP(67), 6)
IED=ICVT(ITEMP(73), 6)
IYC=19
IXC=25
DO 100 I= 1,4
  XCOR(I)=FLOAT(ICVT(ITEMP(IXC),6))*XSCALE
  YCOR(I)=FLOAT(ICVT(ITEMP(IYC),6))*YSCALE
  IXC=IXC+12
  IYC=IYC+12
100  CONTINUE
RETURN
DATA XSCALE / 1.00 /, YSCALE / 1.00 /
END
```


UP = Z2 + ((XOBS-X2)/GRIDR) * (Z3-Z2)
C ***
ELVOBS = DOWN + ((YOBS-Y1)/GRIDR) * (UP-DOWN)
RETURN
END

```
SUBROUTINE FDTATR (IA,N)
C ***
C   BY MONTE COLEMAN
C   CONVERTS FIELD DATA CHARACTERS TO DISPLAY CODE
C ***
C   DIMENSION IA(1), IB(64)
DO 100 I=1,N
    J=IA(I)+1
    IA(I)=ID(J)
100   CONTINUE
      RETURN
C   FIELD DATA TO DISPLAY CODE TABLE
DATA ID / 0, 47, 50, 0, 0, 45, 1, 2,
*           3, 4, 5, 6, 7, 8, 9, 10,
*           11, 12, 13, 14, 15, 16, 17, 13,
*           10, 20, 21, 22, 23, 24, 25, 26,
*           42, 38, 37, 50, 44, 59, 0, 43,
*           39, 41, 51, 0, 0, 0, 46, 0,
*           27, 28, 29, 30, 31, 32, 33, 34,
*           35, 36, 52, 0, 40, 47, 0, 0 /
```

END

```
SUBROUTINE FRCSEN(XTGT, YTGT, IFGSYM)
C ***
C   BY BARBARA BRUNOE
C   GETS NUMERATOR AND DENOMINATOR FOR CALCULATING FRACTION OF AREA
C   OF INTEREST SEEN BY OBSERVER - CONSIDERING VARIOUS TARGET HEIGHTS
C ***
COMMON /PLTSTF/ MAPID, SCALE, NPLHTH, PLTHHT(10), INBS, INK
COMMON /ASNSTF/ RNUM(10), DENOM
COMMON /BOX/ BOXMIN, BOXMAX, BOYMIN, BOYMAX, IBOX
C ***
C   IF YOU AREN'T IN AREA OF INTEREST, DON'T DO ANYTHING - JUST RETURN
C ***
IF ((XTGT .LT. BOXMIN) .OR. (XTGT .GT. BOXMAX) .OR.
     * (YTGT .LT. BOYMIN) .OR. (YTGT .GT. BOYMAX)) RETURN
C ***
C   IF YOU CAN'T SEE ANY TARGETS, ADD 1 TO DENOMINATOR THEN RETURN
C ***
IF (IFGSYM .GT. NPLHTH) DENOM = DENOM + 1
IF (IFGSYM .GT. NPLHTH) RETURN
C ***
C   INCREASE NUMERATOR FOR EACH TARGET HEIGHT THAT CAN BE SEEN,
C   INCREASE DENOMINATOR, THEN RETURN
C ***
DO 100 I = IFGSYM, NPLHTH
      RNUM(I) = RNUM(I) + 1
100   CONTINUE
      DENOM = DENOM + 1
      RETURN
      END
```

```

SUBROUTINE FESTIM(XTOT, LHONHI, HONHI, ICOL1)
C ***
C BY BARBARA BROOME
C CALCULATES HONHI FOR SCANS CLOSEST TO OBSERVER
C ***
COMMON /ZS/ ZOLD(4000), ZNOW(4000), ZLATER(4000)
COMMON /AREA/ XORIGN, YORIGN, XSTOP, YSTOP
COMMON /SEE/ XDBS, YDBS, HDBS, DBTRAN
COMMON /SCANS/NX, NY
COMMON /GRIDR/
DIMENSION HONHI(1)
REAL LHONHI(1)

C ***
C FIND SCANS CLOSEST TO OBSERVER, LEFT IS ZOLD, RIGHT IS ZNOW
C ***
ICOL1 = INT((XDBS - XORIGN + .00001) / GRIDR) + 2
CALL READNS(2, ZNOW(1), NY, ICOL1)
CALL READNS(2, ZOLD(1), NY, ICOL1-1)

C ***
C FIND HONHI FOR PTS. ABOVE OBSERVER ON BOTH SCANS
C ***
C *** FIRST TWO
ITGT1 = INT((YDBS - YORIGN + .00001) / GRIDR) + 2
IF (ITGT1 .GT. NY) GO TO 125
XTGT = XORIGN + (ICOL1 - 1) * GRIDR
YTGT = YORIGN + (ITGT1 - 1) * GRIDR
HONHI(ITGT1) = INT(TVEC(ZNOW(ITGT1)))
ZLATER(ITGT1) = INT(ZNOW(ITGT1))
LHONHI(ITGT1) = INT(TVEC(ZOLD(ITGT1)))
ZOLD(ITGT1) = INT(ZOLD(ITGT1))
ITGTP1 = ITGT1 + 1
IF (ITGTP1 .GT. NY) GO TO 125
XTGT = XTGT - GRIDR

C *** ALL OTHERS
DO 100 ITGT = ITGTP1, NY
    YTGT = YTGT + GRIDR
C *** RIGHT OF OBSERVER
    XTGT = XTGT + GRIDR
    ZP = ZPRIME(XTGT, YTGT, ITGT, ZULL, ZLATER)
    HONHI(ITGT) = ZP - ZNOW(ITGT) + TVEC(ZNOW(ITGT))
    ETVEC = INT(TVEC(ZNOW(ITGT)))
    HONHI(ITGT) = AMAX1(HONHI(ITGT), ETVEC)
    EZNOW = INT(ZNOW(ITGT))
    ZLATER(ITGT) = AMAX1(ZP, EZNOW)

C *** LEFT OF OBSERVER
    XTGT = XTGT - GRIDR
    ZP = ZPRIME(XTGT, YTGT, ITGT, ZLATER, ZOLD)
    LHONHI(ITGT) = ZP - (ZOLD(ITGT) - TVCC(ZULL(ITGT)))
    ETVEC = INT(TVEC(ZOLD(ITGT)))
    LHONHI(ITGT) = AMAX1(LHONHI(ITGT), ETVEC)
    LZOLD = INT(ZOLD(ITGT))
    ZOLD(ITGT) = AMAX1(ZP, LZOLD)
100    CONTINUE

C ***
C FIND HONHI FOR PTS. BELOW OR LEVEL WITH OES. ON BOTH SCANS
C ***

```

```

C *** FIRST TWO
125 ITGTM1 = ITGT1 - 1
    XTGT = XORIGN + (ICOL1 - 1) * GRIDR
    YTGT = YORIGN + (ITGTM1 - 1) * GRIDR
C *** POINTS HORIZONTAL TO OBS., IF THEY EXIST
    IF (ABS(YTGT - YOBS) .GT. .00001) GO TO 150
    HOWHI(ITGTM1) = INT(TVEG(ZH0W(ITGTM1)))
    ZLATER(ITGTM1) = INT(ZH0W(ITGTM1))
    LH0WHI(ITGTM1) = INT(TVEG(ZOLD(ITGTM1)))
    ZOLD(ITGTM1) = INT(ZOLD(ITGTM1))
    ITGTM1 = ITGTM1 - 1
    XTGT = XORIGN + (ICOL1 - 1) * GRIDR
    YTGT = YORIGN + (ITGTM1 - 1) * GRIDR
    IF (ITGTM1 .LT. 1) GO TO 300
C *** FIRST TWO BELOW
150 HOWHI(ITGTM2) = INT(TVEG(ZH0W(ITGTM1)))
    ZLATER(ITGTM1) = INT(ZH0W(ITGTM1))
    LH0WHI(ITGTM1) = INT(TVEG(ZOLD(ITGTM1)))
    ZOLD(ITGTM1) = INT(ZOLD(ITGTM1))
    ITGTM2 = ITGTM1 - 1
    ETGT = ITGTM1
    XTGT = ETGT - GRIDR
    IF (ITGTM2 .LT. 1) GO TO 300
C *** ALL OTHERS
DU 200 J = 1, ITGTM2
    ITGT = ITGT - 1
    YTGT = YTGT - GRIDR
C *** RIGHT OF OBSERVER
    XTGT = XTGT + GRIDR
    ZP = ZPRIME(XTGT, YTGT, ITGT, ZOLD, ZLATER)
    HOWHI(ITGT) = ZP - (ZH0W(ITGT) - TVEG(ZH0W(ITGT)))
    ETVEG = INT(TVEG(ZH0W(ITGT)))
    HOWHI(ITGT) = AMAX1(HOWHI(ITGT), ETVEG)
    EZH0W = INT(ZH0W(ITGT))
    ZLATER(ITGT) = AMAX1(ZP, EZH0W)
C *** LEFT OF OBSERVER
    XTGT = XTGT - GRIDR
    ZP = ZPRIME(XTGT, YTGT, ITGT, ZLATER, ZOLD)
    LH0WHI(ITGT) = ZP - (ZOLD(ITGT) - TVEG(ZOLD(ITGT)))
    ETVEG = INT(TVEG(ZOLD(ITGT)))
    LH0WHI(ITGT) = AMAX1(LH0WHI(ITGT), ETVEG)
    LZOLD = INT(ZOLD(ITGT))
    ZOLD(ITGT) = AMAX1(ZP, LZOLD)
200 CONTINUE
300 RETURN
END

```

```
C *** SUBROUTINE GOZIN2(RLITL,BIG,LITNAM,BIGNAM)
C   BY BARBARA BROOME
C   MAKES SURE RLITL GOES INTO BIG (WITH NO REMAINDER).
C   LITNAM = 'RLITL', BIGNAM = 'BIG'.
C ***
      IF ((AINT(BIG/RLITL)*RLITL) .NE. BIG) WRITE(6,100)
      *          BIGNAM,LITNAM,BIGNAM,BIG,LITNAM,RLITL
      *          IF ((AINT(BIG/RLITL)*RLITL) .NE. BIG) STOP
      *          RETURN
100 FORMAT(1X, A6, ' SHOULD BE DIVISIBLE BY ', A6, '/',
      *          1X, A6, ' = ', F10.3, '/',
      *          1X, A6, ' - ', F10.3)
      END
```

```
FUNCTION ICVT (IBUF, N)
C ***
C BY MONTE COLEMAN
C RETURNS INTERNAL INTEGER VALUE ASSOCIATED WITH N 6-BIT BYTES
C STORED ONE PER WORD IN ARRAY IBUF.
C ***
DIMENSION IBUF(1)
INTEGER SHIFT
IF (N .GT. 10) GO TO 200
ITEM=0
C
DO 100 I=1,N
    ITEM=SHIFT(ITEM,6).OR.IBUF(I)
100    CONTINUE
ICVT=ITEM
RETURN
C
200 PRINT 210, N
STOP
210 FORMAT (' ICVT/ERROR.....LARGE N, N=', I10)
END
```

```
SUBROUTINE IMNMX(IVALUE,IMIN,IMAX,VALNAM,MINNAM,MAXNAM)
C *** BY BARBARA BROOME
C MAKES SURE IMIN IS LESS THAN IVALUE IS LESS THAN IMAX.
C VALNAM = 'IVALUE', MINNAM = 'IMIN', MAXNAM = 'IMAX'.
C ***
      IF (IVALUE .LE. IMIN) WRITE(6,100) VALNAM,MINNAM,VALNAM,
      *                                     IVALUE,MINNAM,IMIN
      IF (IVALUE .GE. IMAX) WRITE(6,200) VALNAM,MAXNAM,VALNAM,
      *                                     IVALUE,MAXNAM,IMAX
      IF (IVALUE .LE. IMIN) STOP
      IF (IVALUE .GE. IMAX) STOP
      RETURN
100 FORMAT(1X, A20, ' SHOULD BE GREATER THAN ', A20,/,,
      *           1X, A20, ' = ', I10, /,
      *           1X, A20, ' = ', I10)
200 FORMAT(1X, A20, ' SHOULD BE LESS THAN ', A20,/,,
      *           1X, A20, ' = ', I10, /,
      *           1X, A20, ' = ', I10)
END
```

```
FUNCTION LFRACT(Z,K)
C ***
C   BY ARTHUR GROVES
C   THIS FUNCTION RETURNS TEN TIMES THE FRACTIONAL PART OF THE
C   K-TH (OF THREE) ELEVATIONS PACKED INTO THE WORD Z.
C ***
A=AINT(Z)
C=A
IF(K.EQ.1)GOTO 1
A=10000.*(Z-A)
C=AINT(A)
IF(K.EQ.2)GOTO 1
C=10000.*(A-C)
C=AINT(C)
1 C=.1*C + .001
A=C-AINT(C)
B=-.05
DO 2 I=1,4
B=B+.1
IF(A.GT.B)GOTO 2
LFRACT=I-1
RETURN
2 CONTINUE
END
```

```
FUNCTION LOCATE(X,X0,G)
C ***
C      BY ARTHUR GROVES
C      THIS FUNCTION RETURNS THE NUMBER OF GRID POINTS WHOSE ORDINATES
C      ARE LESS THAN OR EQUAL TO X. X0 (INPUT) IS THE ORDINATE OF THE
C      FIRST GRID POINT, AND G (INPUT) IS THE SPACING BETWEEN GRID POINTS
C ***
LOCATE=AINT((X-X0)/G+1.)
RETURN
END
```

```

SUBROUTINE MERGIT(NTAPES, TGRID, GRIDR, XMIN, XMAX, YMIN, YMAX, NX,
$                               NY, XORIGN, YORIGN, XSTOPP, YSTOPP)
C ***
C   BY ARTHUR GROVES AND BARBARA BROOME
C   MERGE UP TO 12 DMA TAPES. ELEVATIONS GO IN DIRECT ACCESS ARRAY.
C ***
DIMENSION MINDEX(4001)
DIMENSION BUF(4000)
DIMENSION L(12), XO(12), YO(12), R(8000), XC(4), YC(4)
DIMENSION XL(12,5), YL(12,5), XCM(4), YCM(4), C(4)
COMMON /VEGIND/ JVEG
DATA (C(I),I=1,4)/"SOUTHWEST", "NORTHWEST", "NORTHEAST", "SOUTHEAST"/
CALL OPENAS(2, MINDEX, 4001, 0)

C ***
C   COMPUTE THINNING CONSTANT
C ***
ISKIP = AINT(GRIDR/TGRID + .1)
IBIG = 1000000000
C ***
C   READ HEADER RECORDS. COMPUTE INDIVIDUAL AND COMBINED TAPE START
C ***
XSTART = 1000000000.
YSTART = 1000000000.
DO 100 I=1,NTAPES
  K = I + 6
  IF (I .GT. 6) K = I + 7
  CALL RDDATA(K, ICODE)
  CALL RTYPRC(ICODE, 1)
  CALL DCTID(ISH, ISER, IED, XC, YC)
  DO 50 N=1,4
    XL(I,N)=XC(N)
    YL(I,N)=YC(N)
  CONTINUE
  XL(I,5)=XC(1)
  YL(I,5)=YC(1)
  XO(I) = AMINI(XC(1), XC(2))
  YO(I) = AMINI(YC(1), YC(4))
  XSTART = AMINI(XSTART, XO(I))
  YSTART = AMINI(YSTART, YO(I))
  CALL RDDATA(K, ICODE)
  CALL RTYPRC(ICODE, 2)
  L(I) = 0
100  CONTINUE
C ***
C   CHECK TO SEE IF EACH CORNER OF THE AREA TO BE MERGED
C   IS ON ONE OF THE TAPES.
C ***
XCM(1)=XMIN
XCM(2)=XMIN
XCM(3)=XMAX
XCM(4)=XMAX
YCM(1)=YMIN
YCM(2)=YMAX
YCM(3)=YMAX
YCM(4)=YMIN
NCOT=0
DO 175 K=1,4

```

```

      DD 150 I=1,NTAPES
      NOR=0
      DD 125 N=1,4
      $           D=XCH(K)*(YL(I,N)-YL(I,N+1))
      $           -YCH(K)*(XL(I,N)-XL(I,N+1))
      $           -XL(I,N+1)*YL(I,N)+XL(I,N)*YL(I,N+1)
      $           IF(D.LE.0.)NOR=NOR+1
      125         CONTINUE
      150         IF(NOR.EQ.4)GOTO 175
      150         CONTINUE
      NCOT=NCOT+1
      WRITE(6,40)C(K)
      175         CONTINUE
      C *** COMPUTE Y COORDINATE OF 1ST POINT ON EACH MERGED SCAN LINE
      C ***
      Y = YSTART - TGRID
      DO 200 I=1,IBIG
      IF ((Y .LE. YMIN) .AND. (Y+TGRID .GT. YMIN)) GO TO 300
      Y = Y + TGRID
      200         CONTINUE
      300 YORIGN = Y
      ISAVE = I - 1
      C *** COMPUTE NUMBER OF POINTS ON EACH MERGED SCAN LINE
      C ***
      DO 400 I=2,IBIG
      Y = Y + GRIDR
      IF ((Y-GRIDR .LE. YMAX) .AND. (Y .GT. YMAX)) GO TO 500
      400         CONTINUE
      500 NY = I
      C ***
      C SET UP LOOP TO CYCLE THROUGH INCREASING VALUES OF X
      C ***
      X = XSTART - TGRID
      XLAST = XSTART - GRIDR
      IX = J
      DO 900 I=1,I8IG
      JIM = 0
      X = X + TGRID
      IF (X .GT. XMAX+GRIDR) GO TO 1000
      C ***
      C CYCLE THRU THE TAPES PICKING OFF DATA FROM EACH TAPE
      C THAT CORRESPONDS TO THE CURRENT VALUE OF X
      C ***
      DD 800 J=1,NTAPES
      K = J + 6
      IF (J .GT. 6) K = J + 7
      IF ((X .LT. XO(J)-.1) .OR. (L(J).EQ.1)) GO TO 800
      CALL RDDATA(K, ICODE)
      IF ((ICODE.NE.'EOF') .AND. (ICODE.NE.'END')) GO TO 600
      L(J) = 1
      GO TO 800
      600         IF (ICODE .EQ. 'DATA') GO TO 700
      IUNIT = J + 6
      WRITE(6,10) IUNIT
      STOP

```

```

700      IF ((X.LT.XMIN-TGRID).OR.(X-XLAST.LT.GRIDR-1.)) GO TO 800
        JIM = 1
        CALL DCDMAX(XX, YY, NREC)
        IY = YY
        M = AINT((Y0(J)-YSTART)/TGRID + .1)
        CALL STDATA(R,M+IY+1,8000,JVEG)
        CNTINUE
C     0NL
C     *** THIN AND RECORD THE ELEVATION DATA FOR THIS SCAN LINE.
C     COMPUTE NUMBER OF SCANS AND X ORIGIN OF MERGED DATA.
C     ***
C     IF (JIM .EQ. 0) GO TO 9NU
        NX = NX + 1
        IF (NX .EQ. 1) XORIGN = X
        XLAST = X
        IISAVE = ISAVE + (NY-1)*ISKIP
        ICOUNT = 1
        DO 850 J=ISAVE, NSAVE, ISKIP
            BUF(ICOUNT) = R(J)
            ICOUNT = ICOUNT + 1
        850    CONTINUE
        CALL WRITHS(2, BUF(1), NY, NX)
        910    CONTINUE
C     ***
C     WRITE IDENTIFYING DATA FOR MERGED TAPE
C     ***
C     1000 XSTOP = XORIGN + GRIDR*FLOAT(NX-1)
        YSTOP = YORIGN + GRIDR*FLOAT(NY-1)
        WRITE(6,20) NX, NY, XORIGN, YORIGN, XSTOP, YSTOP, GRIDR
        RETURN
C     ***
C     FORMATS
C     ***
10 FORMAT(' SOMETHING NON-STANDARD ABOUT RECORD FORMAT ON UNIT', I1.)
2L FORMAT(//, ' MERGED ARRAY', /,
$      ' NUMBER OF SCAN LINES =', I10, /,
$      ' NUMBER OF POINTS PER SCAN LINE =', I10, /,
$      ' X COORDINATE OF FIRST SCAN LINE =', F10.1, /,
$      ' Y COORDINATE OF FIRST POINT ON EACH SCAN LINE =', F10.1, /,
$      ' X COORDINATE OF LAST SCAN LINE =', F10.1, /,
$      ' Y COORDINATE OF LAST POINT ON EACH SCAN LINE =', F10.1, /,
$      ' ARRAY GRID =', F10.1)
30 FORMAT(//, ' RECORD', I10, /,
$      (' ', 10F7.1))
40 FORMAT(/1X,A10,'CORNER OF AREA NOT ON ANY TAPE - RUN ABORTED
$')
        END

```

```

SUBROUTINE ONELN(ICOL, HOWHI)
C ***
C BY BARBARA BROOME
C GIVEN ARRAYS ZOLD (MAX PREVIOUS INTERRUPT) & ZNOW (CURRENT DMA
C ELEVATIONS PLUS VEGETATION HEIGHT AND VEGETATION CODE)
C CALCULATES FOR ONE SCAN HOW HIGH TGT MUST BE RAISED TO BE
C SEEN & UPDATED MAX INTERRUPT (ZLATER).
C ***
COMMON /ZS/ ZOLD(4000), ZNOW(4000), ZLATER(4000)
COMMON /AREA/ XORIGN, YORIGN, XSTOP, YSTOP
COMMON /SEE/ XOBS, YOBS, HOBS, OBTRAN
COMMON /SCANS/ NX, NY
COMMON GRIDR
DIMENSION HOWHI(1)

C ***
C SPECIAL CASE: OBSERVER ON A SCAN LINE
C ***
XTGT = XORIGN + (ICOL - 1) * GRIDR
IF (ABS(XTGT - (XOBS-GRIDR)) .GT. .00001) GO TO 50
ITGT1 = INT((YOBS - YORIGN + .00001) / GRIDR) + 2
YTGT = YORIGN + (ITGT1 - 1) * GRIDR
ITGTM1 = ITGT1 - 1
ITGTM2 = ITGT1 - 2
IF (ITGT1 .GT. NY) GO TO 25
HOWHI(ITGT1) = INT(TVEG(ZNOW(ITGT1)))
ZLATER(ITGT1) = INT(ZNOW(ITGT1))
25 IF (ITGTM1 .LT. 1) GO TO 50
HOWHI(ITGTM1) = INT(TVEG(ZNOW(ITGTM1)))
ZLATER(ITGTM1) = INT(ZNOW(ITGTM1))
IF (ITGTM2 .LT. 1) GO TO 50
IF (ABS(YTGT - (YOBS+GRIDR)) .GT. .00001) GO TO 50
HOWHI(ITGTM2) = INT(TVEG(ZNOW(ITGTM2)))
ZLATER(ITGTM2) = INT(ZNOW(ITGTM2))

C ***
C POINTS ABOVE OBSERVER
C ***
50 ITGT1 = INT((YOBS - YORIGN + .00001) / GRIDR) + 2
IF (ABS(XTGT - (XOBS-GRIDR)) .LT. .00001) ITGT1 = ITGT1 + 1
XTGT = XORIGN + (ICOL - 1) * GRIDR
YTGT = YORIGN + (ITGT1 - 1) * GRIDR
IF (ITGT1 .GT. NY) GO TO 150
DO 100 ITGT = ITGT1, NY
    ZP = ZPRIME(XTGT, YTGT, ITGT, ZOLD, ZLATER)
    HOWHI(ITGT) = ZP - (ZNOW(ITGT) - TVEG(ZNOW(ITGT)))
    ETVEG = INT(TVEG(ZNOW(ITGT)))
    HOWHI(ITGT) = AMAX1(HOWHI(ITGT), ETVEG)
    EZNOW = INT(ZNOW(ITGT))
    ZLATER(ITGT) = AMAX1(ZP, EZNOW)
    YTGT = YTGT + GRIDR
100 CONTINUE

C ***
C POINTS BELOW OBSERVER
C ***
150 ITGTM1 = ITGT1 - 1
IF (ABS(XTGT - (XOBS-GRIDR)) .LT. .00001) ITGTM1 = ITGT1 - 3
YTGT = YORIGN + (ITGTM1 - 1) * GRIDR

```

```
IF (ABS(YTGT - (Y0BS-GRIDR)) .LT. .00001) ITGTM1 = ITGT1 - 4
IF (ITGTM1 .LT. 1) GO TO 300
ITGT = ITGTM1 + 1
YTGT = YORIGN + (ITGT - 1) * GRIDR
DO 200 I = 1, ITGTM1
    ITGT = ITGT - 1
    YTGT = YTGT - GRIDR
    ZP = ZPRIME(XTGT, YTGT, ITGT, ZOLD, ZLATER)
    HOWHI(ITGT) = ZP - (ZNOW(ITGT) - TVEG(ZNOW(ITGT)))
    ETVEG = INT(TVEG(ZNOW(ITGT)))
    HOWHI(ITGT) = AMAX1(HOWHI(ITGT), ETVEG)
    EZNOW = INT(ZNOW(ITGT))
    ZLATER(ITGT) = AMAX1(ZP, EZNOW)
200    CONTINUE
300    RETURN
      END
```

```

      SUBROUTINE PLTICS(IXRYAX, BOTRLF, START, STOP)
C *** BY ARTHUR GROVES AND BARBARA BROOME
C THIS ROUTINE PUTS LARGER TIC MARKS ALONG AN AXIS
C IXRYAX - INDICATES WHETHER MARKING X- OR Y-AXIS (-X , +Y)
C BOTRLT - GIVES THE BOTTOM OR LEFT (DEPENDING ON IXRYAX) TIC
C           IF IXRYAX=0, GIVES BOTTOM; ELSE GIVES LEFT
C START - STARTING COORDINATE ON AXIS
C STOP - STOPPING COORDINATE ON AXIS
C ***
C       DIMENSION EKS(2), WYE(2)
C ***
C       TO LABEL X-AXIS
C ***
C       IF (IXRYAX .EQ. 1) GO TO 200
C       WYE(1) = BOTRLF
C       WYE(2) = BOTRLF + 60.
C       DO 100 I = 1, 1000
C           EKS(1) = START + 10LJ.*FLDAT(I-1)
C           EKS(2) = EKS(1)
C           IF ((EKS(1)-STOP) .GT. 50.) RETURN
C           CALL PLTDTS(1, 0, EKS, WYE, 2, 1)
C 100   CONTINUE
C       RETURN
C ***
C       TO LABEL Y-AXIS
C ***
C 200   EKS(1) = ROTRLF
C       EKS(2) = ROTRLF + 60.
C       DO 300 I = 1, 1000
C           WYE(1) = START + 10LJ.*FLDAT(I-1)
C           WYE(2) = WYE(1)
C           IF ((WYE(1)-STOP) .GT. 50.) RETURN
C           CALL PLTDTS(1, 0, EKS, WYE, 2, 1)
C 300   CONTINUE
C       RETURN
C END

```

```

SUBROUTINE PLTLN(HOWHI, ICOL, ITGTAV)
C ***
C BY BARBARA BROOME
C PLOTS ONE SCAN LINE OF HOWHI'S (ODD COLUMNS UP OTHERS DOWN)
C IF KEEPING UP WITH FRAC. OF BOX SEEN, CALL NEC. SUBROUTINE
C ***
DIMENSION XPLOT(2), YPLOT(2)
DIMENSION SYMBOL(10)
DIMENSION HOWHI(4000)
COMMON /ZS/ ZOLD(4000), ZNOW(4000), ZLATER(4000)
COMMON /AREA/ XORIGN, YORIGN, XSTOP, YSTOP
COMMON /SCANS/ NX, NY
COMMON GRIDR
COMMON /PLTSTF/ MAPID, SCALE, NPLHT, PLHT(10), INBS, INK
COMMON /BOX/ BOXMIN, BOXMAX, BOYMIN, BOYMAX, IBOX
DATA SYMBOL /'>','>','>','>','>','>','>','>','>','>'/
* SCLCNV = SCALE/100.
HIGH = .45*GRIDR
WIDE = .2808*GRIDR
SIZE = .9*GRIDR / SCLCNV
D = .5*GRIDR
IF(MOD(ICOL, 2) .EQ. 0) D = -D
XTGT = XORIGN + (ICOL-1)*GRIDR
IF (NPLHT .LE. 1) GO TO 400
C ***
C CASE 1: MULTIPLE TARGET HEIGHTS
C GIVEN SCAN OF HOWHI'S, FIGURE (FOR EACH Y) WHICH SYMBOL TO PLOT
C ***
DO 300 I = 1, NY
  IF (MOD(ICOL, 2) .EQ. 1) J = I
  IF (MOD(ICOL, 2) .EQ. 0) J = NY - I + 1
  YTGT = YORIGN + (J-1)*GRIDR
  DO 100 IFGSYM = 1, NPLHT
    IF (ITGTAV .EQ. 1) HOWHI(J) = HOWHI(J) -
      INT(TVEG(ZNOW(J)))
    * IF (HOWHI(J) .LE. PLHT(IFGSYM)) GO TO 200
100  CONTINUE
  IFGSYM = 11
200  IF(IFGSYM .GT. 1) CALL PLTSYM(SIZE, SYMBOL(IFGSYM-1), 0.,
*                                         XTGT-WIDE, YTGT-HIGH)
    IF (IBOX .NE. 0) CALL FRCSEN(XTGT, YTGT, IFGSYM)
300  CONTINUE
RETURN
C ***
C CASE 2: YES/NO MAP (ONE TARGET HEIGHT)
C XPLOT(1)&(2) AND YPLOT(1)&(2) HOLD START/STOP OF O-O-V SEGMENTS
C EVEN COLUMNS PLOT DOWN, ODD COLUMNS PLOT UP
C ***
400 XPLOT(1) = XORIGN + (ICOL-1)*GRIDR
XPLOT(2) = XPLOT(1)
YPLOT(1) = 0.
YPLOT(2) = 0.
DO 500 I=1,NY
  J = I

```

```

IF (MOD(ICOL,2) .EQ. 0) J = NY - I + 1
YTGT = YORIGN + (J-1) * GRIDR
IF (ITGTAV .EQ. 1) HOWHI(J) = HOWHI(J) -
INT(TVEG(ZNOW(J)))
IF (HOWHI(J) .LE. PLTHT(1)) IFGSYM = 1
IF (HOWHI(J) .GT. PLTHT(1)) IFGSYM = 99999
IF (IBOX .NE. 0) CALL FRCSEN(XTGT, YTGT, IFGSYM)
IF ((YPLOT(1) .LE. 0.) .AND. (HOWHI(J) .GT. PLTHT(1)))
YPLOT(1) = YORIGN + (J-1)*GRIDR - D
IF (YPLOT(1) .LE. 0.) GO TO 500
IF (HOWHI(J) .LE. PLTHT(1))
YPLOT(2) = YORIGN + (J-1)*GRIDR - D
IF (I .EQ. NY)
YPLOT(2) = YORIGN + (J-1)*GRIDR + D
IF (YPLOT(2) .LE. 0.) GO TO 500
CALL PLTDTS(1, 0, XPLOT, YPLOT, 2, 0)
YPLOT(1) = 0.
YPLOT(2) = 0,
500   CONTINUE
      RETURN
      END

```

```

SUBROUTINE PLTPRE(XMIN, XMAX, YMIN, YMAX)
C ***
C BY BARBARA BROOME
C PLOTS PRELIMINARY INFORMATION - BEFORE LOS CALCULATIONS
C ***
DIMENSION PHTS(2)
DIMENSION POBS(5)
DIMENSION PLB(6)
DIMENSION MID(2)
DIMENSION LABELP(3), LABELI(4), SYMBOL(10)
DIMENSION LGND1(1), LGND2(3), LGND3(3), LGND4(2), LGND5(3)
COMMON /PLTSTY/ MAPID, SCALE, NPLHTT, PLHTT(10), IOBS, INK
COMMON /SEE/ XOBS, YOBS, HOBS, OBTRAN
DATA LABELP //BROOME 1, 'BLDG 392 1, 'X2417 1/
DATA LABELI //BROOME 1, 'BLDG 392 1, 'X2417 1,
*      'INK PLEASE'/
DATA LGND1 //LEGEND >1/
DATA LGND2 //POSITION W, 'HERE TARGE', 'T >1/
DATA LGND3 //X METERS H, 'IGH OR MOR', 'E >1/
DATA LGND4 //CAN BE SEE, 'N, WHERE >1/
DATA LGND5 //SYMBOL 1, 1, 1, 'X = >1/
DATA SYMBOL//>1, +>1, />1, *>1, 'A>1, 'B>1, 'C>1, 'D>1, 'E>1,
*      'F>1/
C ***
C PLOT AXES
C ***
PXMIN = 1000. * AINT(.001 * (XMIN + .001))
PXMAX = 1000. * AINT(.001 * (XMAX - .001)) + 1000.
PYMIN = 1000. * AINT(.001 * (YMIN + .001))
PYMAX = 1000. * AINT(.001 * (YMAX - .001)) + 1000.
F = SCALE/100.
XPAGE = (PXMAX - PXMIN)/F + 32.
IF (XPAGE .LT. 46.) XPAGE = 46.
YPAGE = (PYMAX - PYMIN)/F + 8.
IF (YPAGE .LT. 21.) YPAGE = 21.
CALL RMNMX(XPAGE, 45.99, 3657., 'XPAGE', 'TITLE PLOT', '12W FT MAX')
CALL RMNMX(YPAGE, 20.9, 73., 'YPAGE', 'LABEL SIZE', '29 IN. MAX')
CALL PLTPGE
IF (INK .EQ. 0) CALL PLTBEG(XPAGE, YPAGE, .3937, 13, LABELP)
IF (INK .EQ. 1) CALL PLTBEG(XPAGE, YPAGE, .3937, 13, LABELI)
CALL PLTSCA(6., 6., PXMIN, PYMIN, F, F)
CALL PLTAXS(1000., 1000., PXMIN, PXMAX, PYMIN, PYMAX, 4)
C ***
C INCREASE PLOT TICMARK SIZE (TOP, RT, BOTTOM, L)
C ***
CALL PLTICS(0, PYMAX, PXMIN, PXMAX)
CALL PLTICS(1, PXMAX, PYMIN, PYMAX)
CALL PLTICS(0, PYMIN-60., PXMIN, PXMAX)
CALL PLTICS(1, PXMIN-60., PYMIN, PYMAX)
C ***
C LABEL AXES
C ***
CALL LABELA(1000., 1000., PXMIN, PXMAX, PYMIN, PYMAX, .001, .001)
C ***
C PLOT MAP IDENTIFICATION
C ***

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```

        ENCODE(20, 900, MID(1)) MAPID
        CALL PLTSYM(.3, MID, 0., PXMIN, PYMAX + .8*F)
C ***
C PLOT OBSERVER
C ***
        CALL PLTDTS(3, 0, XOBS, YOBS, 1, 0)
C ***
C PLOT OBSERVER COORDINATES AND HEIGHT
C ***
        ENCODE(42, 910, POBS(1)) XOBS, YOBS
        CALL PLTSYM(.3, POBS, 0., PXMIN, PYMIN - 2.8*F)
        ENCODE(29, 920, POBS(1)) HOBS
        CALL PLTSYM(.3, POBS, 0., PXMIN, PYMIN - 3.6*F)
        ENCODE(29, 940, POBS(1)) IOBS
        CALL PLTSYM(.3, POBS, 0., PXMIN, PYMIN-4.4*F)
C ***
C PLOT LEGEND
C ***
        CALL PLTSYM(.3, LGND1, 0., PXMAX+7.*F, PYMIN+12.*F)
        CALL PLTSYM(.3, LGND2, 0., PXMAX+7.*F, PYMIN+11.2*F)
        CALL PLTSYM(.3, LGND3, 0., PXMAX+7.*F, PYMIN+10.4*F)
        CALL PLTSYM(.3, LGND4, 0., PXMAX+7.*F, PYMIN+ 9.6*F)
        CALL PLTSYM(.3, LGND5, 0., PXMAX+7.*F, PYMIN+ 8.8*F)
        DO 100 I = 1, NPLHT
          CALL PLTSYM(.3, SYMBOL(I), 0., PXMAX+8.*F,
*                           PYMIN+(8.8-I*.8)*F)
          ENCODE(11, 930, PHTS(1)) PLHT(I)
          CALL PLTSYM(.3, PHTS, 0., PXMAX+13.*F,
*                           PYMIN+(8.8-I*.8)*F)
100      CONTINUE
        ENCODE(53, 980, PLB(1)) PLHT(NPLHT)
        CALL PLTSYM(.3, PLB, 0., PXMAX+8.*F, PYMIN+(8.8-I*.8)*F)
        RETURN
C ***
C FORMATS
C ***
        900 FORMAT('MAP ID - ', A10, '>')
        910 FORMAT('OBSERVER C', 'COORDINATES', ! (' ', F7.0, ! , !, F8.6, ! )>)
        920 FORMAT('OBSERVER H', 'EIGHT = ', F10.2, ')>')
        930 FORMAT(F10.2, ')>')
        940 FORMAT('OBSERVER I', 'D     = ', I10, ')>')
        980 FORMAT('NO TARGET <= ', F10.2, ' METERS HIGH CAN BE SEEN>')
        END

```

```
SUBROUTINE PRFRSN
C ***
C   BY BARBARA BROOME
C   PRINTS THE AVERAGE AREA SEEN FOR EACH TARGET HEIGHT
C ***
COMMON /ASNSTF/ RNUM(10), DENOM
COMMON /PLTSTF/ MAPID, SCALE, NPLHT, PLHT(10), INBS, INK
COMMON /BOX/ BOXMIN, BOXMAX, BOYMIN, BOYMAX, IBOX
WRITE(6, 900) BOXMIN, BOYMIN, BOXMAX, BOYMAX
WRITE(6, 910)
DO 100 I = 1, NPLHT
  CFRACT = PNUM(I) / DENOM
  WRITE(6, 920) CFRACT, PLHT(I)
100    CONTINUE
      RETURN
C ***
C   FORMATS
C ***
900 FORMAT(//, ' AREA OF INTEREST DEFINED BY ', /,
     *        (' (', F10.1, ', ', F10.1, ') '))
910 FORMAT(/, ' FRACTION OF AREA           TARGET', /,
     *        ' VISIBLE TO OBSERVER      HEIGHT', )
920 FORMAT(/, ' ', F10.5, 7X, F10.1)
END
```

```

SUBROUTINE RDDATA(IU,ICODE)
C ***
C BY MONTE COLEMAN
C READS ONE BLOCK FROM A DMA TAPE ON UNIT NUMBER IU AND RETURNS
C ICODE, WHICH INDICATES THE TYPE OF RECORD READ.
C ***
COMMON /DMACOM/ IBUF(700),ITEMP(80),ITEM
INTEGER TID,FID,DTA,EOF,EOI
DATA MSKA / 7777777777770000000B/,MSKB/ 7777770000000000000B/,
*           TID / 0000000000200000000B/,FID / 00000000120000000B/,
*           DTA / 4100000000000000000B/,EOF / 0125462615000000000B/,
*           EOI / 0125513115000000000B/
BUFFER IN (IU,1)(IBUF(1),IBUF(700))
IEOF=UNIT(IU)
IF(IEOF.GT.-1)GOTO 200
100 ITEM=IBUF(1).AND.MSKA
ICODE=' '
IF(ITEM.EQ.TID)ICODE='TAPE ID'
IF(ITEM.EQ.FID)ICODE='FILE ID'
IF(ITEM.EQ.EOF)ICODE='EOF'
IF(ITEM.EQ.EDI)ICODE='EDI'
ITEM=IBUF(1).AND.MSKB
IF(ITEM.EQ.DTA)ICODE='DATA'
IF(ICODE.EQ.' ')GOTO 240
RETURN
200 IF(IEOF.GT.0)GOTO 220
PRINT 210,IU
ICODE='EOF'
RETURN
210 FORMAT(' RDDATA/WARNING.....EOF ON UNIT',I5)
220 PRINT 230,IU
GOTO 100
230 FORMAT(' RDDATA/WARNING.....PARITY ERROR ON UNIT',I5)
240 PRINT 250,ITEM
PRINT 260,IU
260 FORMAT(' ERROR ON TAPE', I10)
STOP
250 FORMAT(' RDDATA/ERROR.....ILLEGAL INDICATOR'/1X,'ICODE= /',02x,
*        ' ')
END

```

SUBROUTINE RDNCCHK

C ***
C BY BARBARA BROOME
C READ, WRITE, AND CHECK INPUT FOR SEEFAR PROGRAM
C MAPID, SCALE, INK - TELLS WHAT MAP TITLE TO PUT ON PLOT,
C WHICH SCALE TO USE & WHETHER TO USE
C BALLPOINT PEN OR INDIA INK
C IOBS, XOBs, YOBs, HOBs, IDNTMV - OBSERVER IDENTIFICATION,
C UTM COORDINATES, HEIGHT, AND INDICATION
C OF WHETHER TO ATTEMPT TO EXPOSE OBSERVER
C NPLTHT, ITGTAV - NO. TGT. HTS. CONSIDERED (LESS OR = 1)
C AND INDICATOR FOR WHETHER HTGT IS HT
C ABOVE VEG (IF 1) OR ABOVE LAND (IF 0)
C PLTHT(I) - I-TH TARGET HEIGHT (METERS)
C XMIN, XMAX, YMIN, YMAX, GRIDR, JVEG
C UTM COORDINATES OF BOUNDARIES
C OF AREA TO BE CONSIDERED & GRID TO USE
C INDICATOR TO ADD VEGETATION
C VEG & URBAN=0, URBAN ONLY=1, NOTHING=2
C NTAPES, TGRID
C IBOX, ISAVE - NUMBER OF DMA TAPES REQUIRED & TAPE GRID
C - CALCULATE VISIBLE FRACTION OF BOX
C (1 = YES, 0 = NO)
C INDICATOR FOR WHETHER TO SAVE HOWHI'S ON
C DISK FOR FUTURE COMPOSITE CALCULATIONS
C (1 = YES, 0 = NO)
C HOWHI AFFECTED BY ITGTAV BEFORE STORING
C BOXMIN, BOXMAX, BOYMIN, BOYMAX - IF IBOX = 1, DESCRIBES
C AREA OF INTEREST
C ***
COMMON /VEGIND/ JVEG
COMMON GRIDR
COMMON /SEE/ XOBs, YOBs, HOBs, OBTRAN
COMMON /PLTSTF/ MAPID, SCALE, NPLTHT, PLTHT(10), IOBS, INK
COMMON /BOX/ BOXMIN, BOXMAX, BOYMIN, BOYMAX, IBOX
COMMON /OTHERI/ IDNTMV, ITGTAV, XMIN, XMAX, YMIN, YMAX, NTAPES,
* TGRID, ISAVE
C ***
C READ AND WRITE INPUT
C ***
READ (5,9UD) MAPID, SCALE, INK
WRITE(6,94C) MAPID, SCALE, INK
READ (5,910) IOBS, XOBs, YOBs, HOBs, IDNTMV
WRITE(6,910) IOBS, XOBs, YOBs, HOBs, IDNTMV
READ (5,96D) NPLTHT, ITGTAV
WRITE(6,96D) NPLTHT, ITGTAV
READ (5,920) (PLTHT(I), I = 1, NPLTHT)
WRITE(6,920) (PLTHT(I), I = 1, NPLTHT)
READ(5,930) XMIN, XMAX, YMIN, YMAX, GRIDR, JVEG
WRITE(6,930) XMIN, XMAX, YMIN, YMAX, GRIDR, JVEG
READ (5,910) NTAPES, TGRID
WRITE(6,910) NTAPES, TGRID
READ (5,96U) IBOX, ISAVE
WRITE(6,96U) IBOX, ISAVE
IF (IBOX .EQ. 1) READ (5,920) BOXMIN, BOXMAX, BOYMIN, BOYMAX
IF (IBOX .EQ. 1) WRITE(6,920) BOXMIN, BOXMAX, BOYMIN, BOYMAX
C ***

```

C      DATA CHECKS
C ***
* CALL RMNMX(SCALE, 4999., 100001., 'SCALE', 'REAS MIN',
*               'REAS MAX')
* CALL IMNMX(INK, -1, 2, 'INK', 'NEG NO',
*               'REAS MAX')
* CALL RMNMX(XOBS, XMIN-.001, XMAX+.001, 'XOBS', 'XMIN', 'XMAX')
* CALL RMNMX(YOBS, YMIN-.001, YMAX+.001, 'YOBS', 'YMIN', 'YMAX')
* CALL RMNMX(HOBS, -.00001, 10001., 'HOBS', 'NEG. NO.', 'REAS MAX')
* CALL IMNMX(IDNTMV, -1, 2, 'IDNTMV', 'NEG. NO.', 'REAS MAX')
* CALL IMNMX(NPLHT, 0, 11, 'NO. OF PLOT HTS.', 'ZERO',
*               'PLOTHT DIM')
* CALL IMNMX(ITGTAV, -1, 2, 'ITGTAV', 'NEG. NO.', 'REAS MAX')
DO 100 I = 1, NPLHT
    CALL RMNMX(PLTHT(I), -.00001, 10001., 'NPLHT(I)', 'NEG NUMBER', 'REAS MAX')
100 CONTINUE
CALL RMNMX(XMIN, 99999., XMAX, 'XMIN', 'REAS MIN', 'XMAX')
CALL RMNMX(XMAX, XMIN, 1000000., 'XMAX', 'XMIN', 'REAS MAX')
CALL RMNMX(YMIN, 999999., YMAX, 'YMIN', 'REAS MIN', 'YMAX')
CALL RMNMX(YMAX, YMIN, 100000000., 'YMAX', 'YMIN', 'REAS MAX')
CALL RMNMX(GRIDR, 0., 1001., 'GRIDR', 'ZERO', 'REAS MAX')
CALL IMNMX(JVEG, -1, 3, 'VEG ADD IN', 'NEG. NO', 'MAX VAL =2')
CALL RMNMX(TGRID, 0., 1001., 'TGRID', 'ZERO', 'REAS MAX')
CALL GOZIN2(TGRID, GRIDR, 'TGRID', 'GRIDR')
CALL IMNMX(NTAPES, 0, 13, 'NTAPES', 'REAS MIN', 'MERGE LIM')
CALL IMNMX(IBOX, -1, 2, 'IBOX', 'NEG. NO.', 'REAS MAX')
IF (IBOX .EQ. 1) CALL RMNMX(BOXMIN, XMIN-.001, BOXMAD, 'BOXMIN',
*                           'XMIN', 'BOXMAX')
* IF (IBOX .EQ. 1) CALL RMNMX(BOXMAX, BOXMIN, XMAX+.001, 'BOXMAX',
*                           'BOXMIN', 'XMAX')
* IF (IBOX .EQ. 1) CALL RMNMX(BOYMIN, YMIN-.001, BOYMAX, 'BOYMIN',
*                           'YMIN', 'BOYMAX')
* IF (IBOX .EQ. 1) CALL RMNMX(BOYMAX, BOYMIN, YMAX+.001, 'BOYMAX',
*                           'BOYMIN', 'YMAX')
CALL IMNMX(ISAVE, -1, 2, 'ISAVE', 'NEG. NO', 'REAS MAX')
RETURN
C ***
C      FORMATS
C ***
900 FORMAT(A10, F10.0, I10)
910 FORMAT(I10, 3F10.0, I10)
920 FORMAT(8F10.0)
930 FORMAT(5F10.0, I10)
940 FORMAT(1X, A10, F10.0, I10)
950 FORMAT(' ELEVATION OF TERRAIN AT OBSERVER POSITION =', F10.1)
960 FORMAT(I10, I10)
END

```

```
SUBROUTINE RMNMX(ZVALUE,ZMIN,ZMAX,VALNAM,MINNAM,MAXNAM)
C *** BY BARBARA BROOME
C MAKES SURE ZMIN IS LESS THAN ZVALUE IS LESS THAN ZMAX.
C VALNAM = 'ZVALUE', MINNAM = 'ZMIN', MAXNAM = 'ZMAX'.
C ***
* IF (ZVALUE .LE. ZMIN) WRITE(6,100) VALNAM,MINNAM,ZMIN,
*                                     ZVALUE,MINNAM,ZMIN
* IF (ZVALUE .GE. ZMAX) WRITE(6,200) VALNAM,MAXNAM,ZMAX,
*                                     ZVALUE,MAXNAM,ZMAX
* IF (ZVALUE .LE. ZMIN) STOP
* IF (ZVALUE .GE. ZMAX) STOP
RETURN
100 FORMAT(1X, A20, ' SHOULD BE GREATER THAN ', A20, /,
*           1X, A20, ' = ', F10.0, /,
*           1X, A20, ' = ', F10.0)
200 FORMAT(1X, A20, ' SHOULD BE LESS THAN ', A20, /,
*           1X, A20, ' = ', F10.0, /,
*           1X, A20, ' = ', F10.0)
END
```

```
SUBROUTINE RTYPRC (ICODE, I)
C ***
C *** BY MONTE COLEMAN
C *** CHECKS TO MAKE SURE INPUT RECOND IS THE RIGHT TYPE
C ***
IF ((I .EQ. 1) .AND. (ICODE .NE. 'TAPE ID')) GOTO 100
IF ((I .EQ. 2) .AND. (ICODE .NE. 'FILE ID')) GOTO 100
IF (ICODE .EQ. 'EOF') GOTO 200
IF (ICODE .EQ. 'EOI') GOTO 300
IF ((I .GT. 2) .AND. (ICODE .NE. 'DATA')) GOTO 100
IF (I .GT. 2500) GOTO 400
RETURN
C ***
C *** THE FIRST 2 RECORDS SHOULD BE FILE ID AND TAPE ID
C ***
100 WRITE(6,150) I,ICODE
150 FORMAT('1RECORD ', I5, ' SHOULD NOT BE A ', A10, ' RECORD.')
STOP
C ***
C *** IF EOF IS ENCOUNTERED
C ***
200 WRITE(6,250) ICODE,I
250 FORMAT(//, ' ', A10, ' ENCONTERED AT RECORD ', I5)
RETURN
C ***
C *** IF EOI IS ENCOUNTERED
C ***
300 WRITE(6,250) ICODE,I
STOP
C ***
C *** IF THERE SEEKS TO BE TOO MANY RECORDS ON THE TAPE
C ***
400 WRITE(6,450)
450 FORMAT('1ARE YOU SURE YOU SHOULD HAVE MORE THAN 2500 SCANLINES?')
STOP
END
```

SUBROUTINE SAVPRE(ITGTAV)

C ***
C BY BARBARA CROOME
C SAVE PRELIMINARY FILE ID INFO IN RECORDS 4001-4013, IF ISAVE = 1.
C ***

COMMON GRIDR
COMMON /SCANS/ NX, NY
COMMON /SEE/ XOBS, YOBS, HOBS, OBTRAN
COMMON /AREA/ XORIGN, YORIGN, XSTOP, YSTOP
COMMON /PLTSTY/ MAPID, SCALE, NPLHT, PLHT(10), IOBS, INK
DIMENSION NINDEX(4015)
CALL OPENHS(3, NINDEX, 4015, 0)
CALL WRITHS(3, XOBS, 1, 4001)
CALL WRITHS(3, YOBS, 1, 4002)
CALL WRITHS(3, HOBS, 1, 4003)
CALL WRITHS(3, XORIGN, 1, 4004)
CALL WRITHS(3, YORIGN, 1, 4005)
CALL WRITHS(3, XSTOP, 1, 4006)
CALL WRITHS(3, YSTOP, 1, 4007)
CALL WRITHS(3, NX, 1, 4008)
CALL WRITHS(3, NY, 1, 4009)
CALL WRITHS(3, GRIDR, 1, 4010)
CALL WRITHS(3, MAPID, 1, 4011)
CALL WRITHS(3, IOBS, 1, 4012)
CALL WRITHS(3, ITGTAV, 1, 4013)
RETURN
END

```

SUBROUTINE STDATA(Z,J,N,JVEG)
C ***
C      BY ARTHUR GROVES
C      STORE ELEVATIONS PLUS VEGETATION PLUS INDICATOR FRACTIONS IN
C      ARRAY Z STARTING AT Z(J). N = DIMENSION OF Z-ARRAY.
C ***
COMMON /DMACOM/ IBUF(700),ITEMP(60),ITEM
DIMENSION Z(1),VEGCOD(4)
INTEGER SHIFT
DATA MSK1/10B/,MSK2/77777B/,VEGCOD/0.0,20.3,10.2,4.1/
I=J
IWORD=2
IGET=1
CALL UNPACK(IBUF(IWORD),ITEMP,60)
IWORD=IWORD+6
100 ISIGN=ITEMP(IGET).AND.MSK1
IVEG=SHIFT(ITEMP(IGET),-4)
ITEM=ICVT(ITEMP(IGET),3).AND. MSK2
IF(ITEM.EQ.0)RETURN
IF(ISIGN.NE.0)ITEM=-ITEM
Z(I)=FLOAT(ITEM)
IF(JVEG.EQ.0)Z(I)=Z(I)+VEGCOD(IVEG+1)
IF(JVEG.EQ.1 .AND. IVEG.EQ.2)Z(I)=Z(I)+VEGCOD(3)
I=I+1
IF(I.GT.N)RETURN
IGET=IGET+3
IF(MOD(IGET,60).NE.1)GOTO 100
CALL UNPACK(IBUF(IWORD),ITEMP,60)
IWORD=IWORD+6
IGET=1
GOTO 100
END

```

FUNCTION TVEG(Z)

C ***
C BY ARTHUR GROVES
C RETURNS VEGETATION AMOUNT ADDED FOR THE GIVEN Z
C ***
DATA ORCHAD /4.1/, URBAN /10.2/, FOREST /20.3/
DPZ = Z - AINT(Z)
TVEG = 0
IF (DPZ .GT. .05) TVEG = ORCHAD
IF (DPZ .GT. .15) TVEG = URBAN
IF (DPZ .GT. .25) TVEG = FOREST
RETURN
END

SUBROUTINE XPOSIT(X,Y,ICARE)

C ***
C BY ARTHUR GROVES
C THE PURPOSE OF THIS SUBROUTINE IS TO ATTEMPT TO MOVE AN OBSERVER
C AT (X,Y) WHICH IS IN VEGETATION/URBAN TO A NEARBY POSITION WHICH
C IS IN THE OPEN. TO HAVE IT DO THIS, CALL THE SUBROUTINE WITH
C ICARE=0. IF IT THEN LOOKS AT THE ELEVATIONS AT THE FOUR CORNERS OF
C THE SQUARE OF ELEVATIONS (X,Y) IS IN. IF NONE OF THESE ARE
C WOODED/URBAN, IT RETURNS THE ORIGINAL (X,Y). IF ALL FOUR CORNERS
C ARE WOODED/URBAN, OR IF EXACTLY ONE PAIR OF OPPOSITE CORNERS ARE
C WOODED/URBAN, IT PRINTS AN APPROPRIATE STATEMENT AND STOPS THE
C RUN, MAKING NO ATTEMPT TO FIND AN OPEN NEARBY LOCATION. IF ONE,
C TWO (ADJACENT) OR THREE CORNERS ARE WOODED/URBAN, IT MOVES THE
C OBSERVER THE LEAST POSSIBLE DISTANCE TO AN ADJACENT SQUARE NOT
C KNOWN TO HAVE ANY WOODED/URBAN CORNERS. IF THIS NEW SQUARE IN
C FACT HAS NO WOODED/URBAN CORNERS, IT RETURNS AS (X,Y) THE NEW
C ADJUSTED OBSERVER LOCATION AND PRINTS THE NEW LOCATION. IF THIS
C NEW SQUARE DOES HAVE ONE OR MORE WOODED/URBAN CORNERS, IT PRINTS
C THAT IT MADE AN UNSUCCESSFUL ATTEMPT TO MOVE THE OBSERVER AND
C THEN STOPS THE RUN. IF THE SUBROUTINE IS CALLED WITH ICARE=1,
C THIS ENTIRE PROCEDURE IS BYPASSED AND (X,Y) IS RETURNED UNCHANGED
C WHETHER OR NOT VEGETATION OR URBAN ARE PRESENT.
C ***
DIMENSION T(4,4)
COMMON GRIDR
COMMON /SCANS/ NX,NY
COMMON /AREA/ XORIGN, YORIGN, XSTOP, YSTOP
COMMON /BIG/ SCAN(4000)
LOGICAL L1,L2,L3,L4
1 FORMAT(' ELEVATIONS REQUIRED FOR XPOZIT NOT PROVIDED BY MERGIT')
2 FORMAT(' OBSERVER MOVED TO (',F10.1,',',',',F10.1,')')
3 FORMAT(' OBSERVER ENTIRELY SURROUNDED BY VEGETATION OR URBAN AND C
* COULD NOT BE MOVED')
4 FORMAT(' EXACTLY ONE PAIR OF OPPOSITE CORNERS IN VEGETATION OR URB
* AN - OBSERVER COULD NOT BE MOVED')
5 FORMAT(' MADE ONE UNSUCCESSFUL ATTEMPT TO MOVE OBSERVER')
C ***
C IF NO ATTEMPT TO MOVE THE OBSERVER IS TO BE MADE, RETURN.
C ***
IF(ICARE, EQ,1)RETURN
C ***
C IDENTIFY THE LOCATION OF THE 4X4 SQUARE OF ELEVATIONS SURROUNDING
C THE OBSERVER.
C ***
IL=LOCATE(X,XORIGN,GRIDR)
JL=LOCATE(Y,YORIGN,GRIDR)
XDRNG = XORIGN + GRIDR * FLOAT(IL-2)
YDRNG = YORIGN + GRIDR * FLOAT(JL-2)
C ***
C IF ALL 16 OF THESE ELEVATIONS HAVE NOT BEEN PROVIDED BY THE
C MERGIT SUBROUTINE, PRINT THAT FACT AND STOP THE RUN.
C ***
IF(IL-1,GE,1,AND,IL+2,LE,NX,AND,JL-1,GE,1,AND,JL+2,LE,NY)GOTO 100
WRITE(b,1)
STOP
C ***

```

C      FILL THE 4X4 ARRAY WITH ELEVATIONS.
C ***
100 DO 120 I=1,4
      CALL READMS(2,SCAN(1),NY,IL+I-2)
      DO 110 J=1,4
          T(I,J)=SCAN(JL+J-2)
110      CONTINUE
120      CONTINUE
C ***
C      CLEAR THE 'SCAN' ARRAY, JUST IN CASE.
C ***
      DO 130 I=1,4000
          SCAN(I)=0,
130      CONTINUE
C ***
C      SET 'MOVED' TO ZERO TO INDICATE THAT (X,Y) IS THE INPUT
C      OBSERVER POSITION AND NOT AN ADJUSTED POSITION.
C ***
      MOVED=0
C ***
C      DETERMINE WHICH CORNERS OF THE 2X2 SQUARE CONTAINING THE CURRENT
C      OBSERVER POSITION ARE IN VEGETATION OR URBAN.  THE APPROPRIATE
C      LOGICAL VARIABLE (L1, L2, L3 OR L4) WILL BE MADE 'TRUE' IF THE
C      CORRESPONDING CORNER IS IN VEGETATION OR URBAN.
C ***
140 I=LOCATE(X,XORIG,GRIDR)
      J=LOCATE(Y,YORIG,GRIDR)
      XSCAN = XORIG + GRIDR * FLOAT(I-1)
      YSCAN = YORIG + GRIDR * FLOAT(J-1)
      L1 = AINT(10.*FRACT(T(I,J)+.00001)) .NE. 0.
      L2 = AINT(10.*FRACT(T(I+1,J)+.00001)) .NE. 0.
      L3 = AINT(10.*FRACT(T(I+1,J+1)+.00001)) .NE. 0.
      L4 = AINT(10.*FRACT(T(I,J+1)+.00001)) .NE. 0.
C ***
C      IF NO CORNERS ARE IN VEGETATION OR URBAN, THE OBSERVER IS IN THE
C      OPEN.  IF THIS IS THE ORIGINAL OBSERVER POSITION, RETURN TO THE
C      CALLING PROGRAM.  IF THIS IS AN ADJUSTED POSITION, WRITE THAT FACT
C      AND THEN RETURN
C ***
      IF(L1.OR.L2.OR.L3.OR.L4)GOTO 150
      IF(MOVED.EQ.1)WRITE(6,2)X,Y
      RETURN
C ***
C      IF MOVED=1 INDICATING THAT THE OBSERVER HAS ALREADY BEEN MOVED
C      TO A NEW LOCATION AND IS STILL IN VEGETATION OR URBAN, WRITE
C      THIS FACT AND STOP THE RUN.
C ***
150 IF(MOVED.EQ.0)GOTO 160
      WRITE(6,5)
      STOP
C ***
C      IF OBSERVER IS ENTIRELY SURROUNDED BY VEGETATION OR URBAN,
C      WRITE THIS FACT AND STOP THE RUN.
C ***
160 IF(.NOT.(L1.AND.L2.AND.L3.AND.L4))GOTO 170
      WRITE(6,3)
      STOP

```

```

C ***
C   IF ONE PAIR OF OPPOSITE CORNERS ARE IN VEGETATION OR URBAN, WITH
C   THE OTHER PAIR IN THE OPEN, WRITE THIS FACT AND STOP THE RUN.
C ***
170 IF(.NOT.(L1.AND.L3.AND..NOT.L2.AND..NOT.L4 .OR. L2.AND.L4.AND.
*   .NOT.L1.AND..NOT.L3))GOTO 180
   WRITE(6,4)
   STOP
C ***
C   THE OBSERVER IS GOING TO BE MOVED TO A NEW LOCATION. AT THIS
C   POINT MAKE 'MOVED' EQUAL 1 SO THAT WHEN CONTROL RETURNS TO
C   STATEMENT 140 TO EXAMINE THE NEW LOCATION, IT WILL RECOGNIZE IT
C   AS A NEW LOCATION.
C ***
180 MOVED=1
C ***
C   MOVE THE OBSERVER IF CORNER NUMBER 1 IS THE ONLY CORNER
C   IN VEGETATION OR URBAN.
C ***
IF(.NOT.(&L1.AND..NOT.L2.AND..NOT.L3.AND..NOT.L4))GOTO 190
D1=XSCAN + GRIDR - X
D2=YSCAN + GRIDR - Y
IF(D1.LT.D2)X=XSCAN + GRIDR + .01
IF(D1.GE.D2)Y=YSCAN + GRIDR + .01
GOTO 140
C ***
C   MOVE THE OBSERVER IF CORNER NUMBER 2 IS THE ONLY CORNER
C   IN VEGETATION OR URBAN.
C ***
190 IF(.NOT.(&.NOT.L1.AND.L2.AND..NOT.L3.AND..NOT.L4))GOTO 200
D1=X - XSCAN
D2=YSCAN + GRIDR - Y
IF(D1.LT.D2)X=XSCAN - .01
IF(D1.GE.D2)Y=YSCAN + GRIDR + .01
GOTO 140
C ***
C   MOVE THE OBSERVER IF CORNER NUMBER 3 IS THE ONLY CORNER
C   IN VEGETATION OR URBAN.
C ***
200 IF(.NOT.(&.NOT.L1.AND..NOT.L2.AND..L3.AND..NOT.L4))GOTO 210
D1=X - XSCAN
D2=Y - YSCAN
IF(D1.LT.D2)X=XSCAN - .01
IF(D1.GE.D2)Y=YSCAN - .01
GOTO 140
C ***
C   MOVE THE OBSERVER IF CORNER NUMBER 4 IS THE ONLY CORNER
C   IN VEGETATION OR URBAN.
C ***
210 IF(.NOT.(&.NOT.L1.AND..NOT.L2.AND..NOT.L3.AND..L4))GOTO 220
D1=XSCAN + GRIDR - X
D2=Y - YSCAN
IF(D1.LT.D2)X=XSCAN + GRIDR + .01
IF(D1.GE.D2)Y=YSCAN - .01
GOTO 140
C ***
C   MOVE THE OBSERVER IF CORNERS NUMBER 1 & 2 ARE THE ONLY

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C CORNERS IN VEGETATION OR URBAN.
C ***
220 IF(.NOT.((L1,AND.,L2,AND.,NOT,L3,AND.,NOT,L4))GOTO 230
Y=YSCAN + GRIDR + .01
GOTO 140
C ***
MOVE THE OBSERVER IF CORNERS NUMBER 1 & 4 ARE THE ONLY
CORNERS IN VEGETATION OR URBAN.
C ***
230 IF(.NOT.((L1,AND.,NOT,L2,AND.,NOT,L3,AND.,L4))GOTO 240
X=XSCAN + GRIDR + .01
GOTO 140
C ***
MOVE THE OBSERVER IF CORNERS NUMBER 2 & 3 ARE THE ONLY
CORNERS IN VEGETATION OR URBAN.
C ***
240 IF(.NOT.((.NOT.,L1,AND.,L2,AND.,L3,AND.,NOT.,L4))GOTO 250
X=XSCAN - .01
GOTO 140
C ***
MOVE THE OBSERVER IF CORNERS NUMBER 3 & 4 ARE THE ONLY
CORNERS IN VEGETATION OR URBAN.
C ***
250 IF(.NOT.((.NOT.,L1,AND.,NOT.,L2,AND.,L3,AND.,L4))GOTO 260
Y=YSCAN - .01
GOTO 140
C ***
MOVE THE OBSERVER IF CORNER 4 IS THE ONLY ONE IN THE OPEN.
C ***
260 IF(.NOT.((L1,AND.,L2,AND.,L3,AND.,NOT.,L4))GOTO 270
X=XSCAN - .01
Y=YSCAN + GRIDR + .01
GOTO 140
C ***
MOVE THE OBSERVER IF CORNER 3 IS THE ONLY ONE IN THE OPEN.
C ***
270 IF(.NOT.((L1,AND.,L2,AND.,NOT.,L3,AND.,L4))GOTO 280
X=XSCAN + GRIDR + .01
Y=YSCAN + GRIDR + .01
GOTO 140
C ***
MOVE THE OBSERVER IF CORNER 2 IS THE ONLY ONE IN THE OPEN.
C ***
280 IF(.NOT.((L1,AND.,NOT.,L2,AND.,L3,AND.,L4))GOTO 290
X=XSCAN + GRIDR + .01
Y=YSCAN - .01
GOTO 140
C ***
MOVE THE OBSERVER IF CORNER 1 IS THE ONLY ONE IN THE OPEN.
C THIS IS THE ONLY CASE LEFT.
C ***
290 X=XSCAN - .01
Y=YSCAN - .01
GOTO 140
END

```

```

FUNCTION ZPRIME(XTGT, YTGT, ITGT, ZOLD, ZLATER)
C ***
C BY BARBARA BROOME
C IF ZPRIME IS GREATER THAN THE TARGET ELEVATION, PREVIOUS TERRAIN
C MUST BE BLOCKING THE VIEW. TGT VISIBLE IFF HOWHI .LE. 0.
C ZOLD ARRAY CONTAINING ELEVATIONS FOR PREVIOUS SCAN (TRUMPED UP).
C ZLATER WILL BE ZOLD FOR NEXT SCAN LINE
C X,Y COORDINATES OF INTERSECT OF OBS-TGT LINE WITH ZOLD SCAN.
C Z INTERPOLATED ELEVATION CORRESPONDING TO POINT (X,Y)
C RE RADIUS OF THE EARTH IN METERS
C ZPRIME PROJECTION OF Z TO TGT POINT
C ***
C *** DIMENSION ZOLD(1), ZLATER(1)
COMMON GRIDR
COMMON /SEE/ XOBS, YOBS, HOBS, DBTRAN
LOGICAL QUAD1U, QUAD1D, QUAD2U, QUAD2D, QUAD3U, QUAD3D,
* QUAD4U, QUAD4D
RE = 6378323.
DX = XTGT - XOBS
DY = YTGT - YOBS
C ***
C DEFINE X, Y, Z AFTER DETERMINING WHICH PORTION OF WHICH QUADRANT
C YOUR TARGET IS IN (8 POSSIBILITIES)
C ***
QUAD1U = (DX .GE. 0.) .AND. (DY .GE. 0.) .AND. (DX .LT. DY)
IF(.NOT., QUAD1U)GO TO 150
X = DX*(DY-GRIDR)/DY + XOBS
Y = YTGT - GRIDR
Z = (1-DX/DY)*ZLATER(ITGT-1) + (DX/DY)*ZOLD(ITGT-1)
GO TO 500
C ***
150 QUAD1D = (DX .GE. 0.) .AND. (DY .GE. 0.) .AND. (DX .GE. DY)
IF(.NOT., QUAD1D)GO TO 200
X = XTGT - GRIDR
Y = DY*(DX-GRIDR)/DX + YOBS
Z = (1-DX/DY)*ZLATER(ITGT) + (DY/DX)*ZOLD(ITGT-1)
GO TO 500
C ***
200 QUAD2U = (DX .LT. 0.) .AND. (DY .GE. 0.) .AND. (-DX .LT. DY)
IF(.NOT., QUAD2U)GO TO 250
X = DX*(DY-GRIDR)/DY + XOBS
Y = YTGT - GRIDR
Z = (1+DX/DY)*ZLATER(ITGT-1) - (DX/DY)*ZOLD(ITGT-1)
GO TO 500
C ***
250 QUAD2D = (DX .LT. 0.) .AND. (DY .GE. 0.) .AND. (-DX .GE. DY)
IF(.NOT., QUAD2D)GO TO 300
X = XTGT + GRIDR
Y = DY*(DX+GRIDR)/DX + YOBS
Z = (1+DY/DX)*ZLOLD(ITGT) - (DY/DX)*ZOLD(ITGT-1)
GO TO 500
C ***
300 QUAD3U = (DX .LT. 0.) .AND. (DY .LT. 0.) .AND. (DX .LT. DY)
IF(.NOT., QUAD3U)GO TO 350
X = XTGT + GRIDR
Y = DY*(DX+GRIDR)/DX + YOBS

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Z = (1-DY/DX)*ZOLD(ITGT) + (DY/DX)*ZOLD(ITGT+1)
GO TO 500
C ***
350 QUAD3D = (DX .LT. 0.) .AND. (DY .LT. 0.) .AND. (DX .GE. DY)
IF(.NOT.,1 QUAD3D) GO TO 400
X = DX*(DY+GRIDR)/DY + X0BS
Y = YTGT + GRIDR
Z = (1-DX/DY)*ZLATER(ITGT+1) + (DX/DY)*ZOLD(ITGT+1)
GO TO 500
C ***
400 QUAD4U = (DX .GE. 0.) .AND. (DY .LT. 0.) .AND. (DX .GT. -DY)
IF(.NOT.,1 QUAD4U) GO TO 450
X = XTGT - GRIDR
Y = DY*(DX-GRIDR)/DX + Y0BS
Z = (1+DY/DX)*ZOLD(ITGT) - (DY/DX)*ZOLD(ITGT+1)
GO TO 500
C ***
450 X = DX*(DY+GRIDR)/DY + X0BS
Y = YTGT + GRIDR
Z = (1+DX/DY)*ZLATER(ITGT+1) - (DX/DY)*ZOLD(ITGT+1)
C ***
500 CONTINUE
C ***
C CALCULATE THE PROJECTION OF Z ONTO THE TARGET POSITION
C ***
RZ = SQRT((X-X0BS)**2 + (Y-Y0BS)**2)
RT = SQRT((XTGT-X0BS)**2 + (YTGT-Y0BS)**2)
B = RE + HOBS + OBTRAN
A = ((RE+Z)*COS(RZ/RE)-RE-HOBS-OBTRAN) / ((RE+Z)*SIN(RZ/RE))
XPRIME = B / (COT(RT/RE)-A)
YPRIME = COT(RT/RE)*B / (COT(RT/RE)-A)
ZPRIME = SQRT(XPRIME**2 + YPRIME**2) - RE
RETURN
END

```

Appendix A2
INPUT FOR SEEFAR PROGRAM

CARD	INPUT	FORMAT	DESCRIPTION
1	MAPID, SCALE, INK	A10,F10.0, I10	<p>MAPID: Alphanumeric map identification. Will be plotted at the top left corner of the map.</p> <p>SCALE: Indicates scale at which to plot map (e.g., 50000. will provide a map plotted at a 1:50000 scale). Subroutine RDNCHK requires 5000. \leq SCALE \leq 100000. Plot paper limits requires map to be less than 64CM high, less than 3657CM wide.</p> <p>INK: If INK = 0 Plot with ballpoint pen. If INK = 1 , plot with india ink.</p>

Appendix A2(Cont'd.)
INPUT FOR SEEFAAR PROGRAM

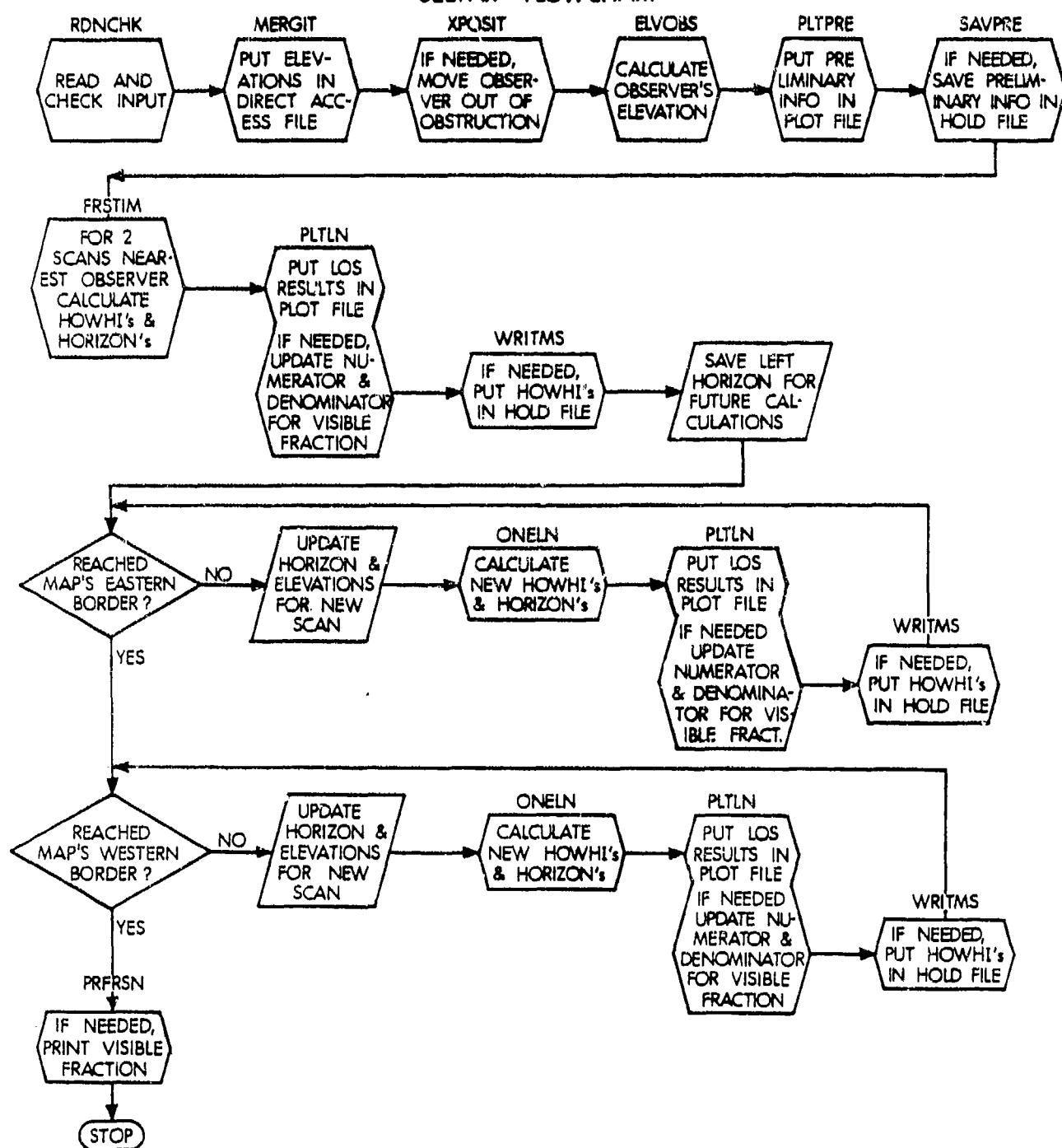
CARD	INPUT	FORMAT	DESCRIPTION
2	I0BS,X0BS,Y0BS,H0BS, IDNTM I10,3F10.0,I10	I0BS: Observer identification number plotted below map. X0BS, Y0BS: Observer UTM coordinates, Observer must be inside map boundaries.	H0BS: Height of observer above terrain (in meters) subroutine RDNCCHK requires $0 \leq H0BS \leq 10000$. IDNTM: Indicates whether to attempt to move observer, should he be just inside a vegetation/urban boundary, to the outside. 0 \Rightarrow move if necessary, 1 \Rightarrow do not move.
3	NPLTHT, ITGTA 2110	NPLTHT: Number of target heights to be considered. Array PLTHT(I) size requires $1 \leq NPLTHT \leq 10$.	ITGTA: Indicates whether target height is the target's height above terrain only (ITGTA=0) or above terrain and any vegetation/urban (ITGTA=1).

CARD	INPUT	FORMAT	DESCRIPTION
4a-4b	PLTHT(I), I=1, NPLHT	8F10.0	<p>PLTHT(I): Lists the target heights (or plot heights) of interest, subroutine RDNCHK requires $0 \leq PLTHT(I) \leq 10000$.</p>
5	XMIN, XMAX, YMIN, YMAX, GRIDR, JVEG	5F10.0, 1I0	<p>XMIN, XMAX, YMIN, YMAX: The four corner UTM coordinates of the map to be plotted (all digits to the nearest meter included).</p> <p>GRIDR: The grid spacing of the resulting line of sight map.</p> <p>JVEG: Indicates whether to ignore vegetation/urban data or not. (0 \Rightarrow include vegetation and urban heights, 1 \Rightarrow include urban heights only, 2 \Rightarrow include neither vegetation nor urban.)</p> <p>Note: STDATA routine is set to add 20 meters for forests (+.3 as indicator), 10 meters for urban (+.2 indicator) and 4 meters for orchards (+.1 indicator) via data statement</p>

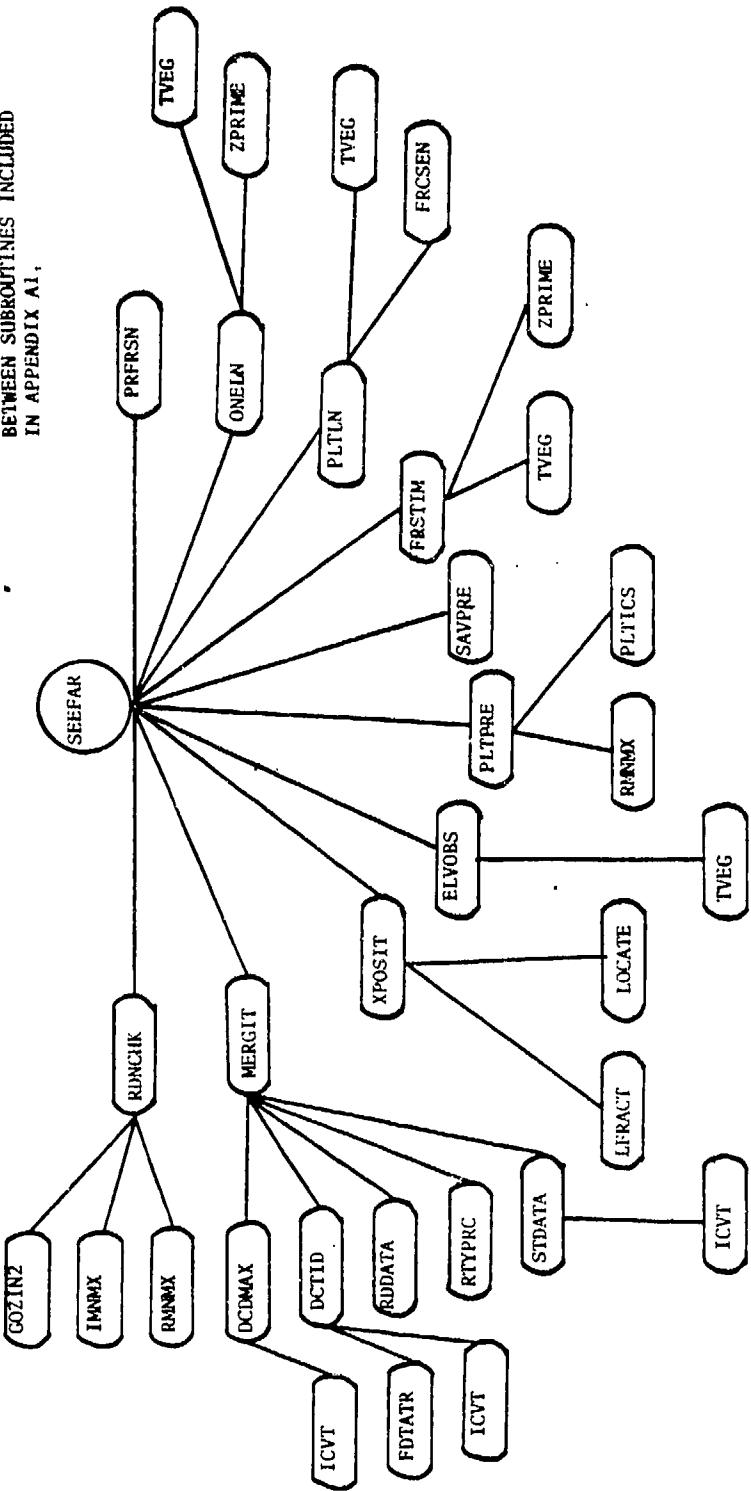
Appendix A2 (Cont'd.)
INPUT FOR SEEFAR PROGRAM

CARD	INPUT	FORMAT	DESCRIPTION
6	NTAPES, TGRID	I10,F10.0	<p>NTAPES: The number of DMA tapes to be merged. Array dimensions in MERGIT require $1 \leq NTAPES \leq 12$</p> <p>TGRID: The grid spacing of the input DMA terrain tapes, generally 12.5 or 25.</p>
7	IBOX, ISAVE	2I10	IBOX: Indicates whether there is a box of interest (IBOX=1) for which one wishes to calculate the visible fraction or not (IBOX=0).
8	BOXMIN, BOXMAX, BOYMIN, (Needed only if IBOX=1) BOYMAX	4F10.0	BOXMIN, BOXMAX, BOYMIN, BOYMAX: The four corner UTM coordinates for the area of interest referred to when IBOX = 1.

**APPENDIX A3
SEEFAR FLOWCHART**



APPENDIX A4
PROGRAM SKELTON: ILLUSTRATES THE RELATIONSHIP
BETWEEN SUBROUTINES INCLUDED
IN APPENDIX A1.



IN ADDITION TO THESE: SUBROUTINES THE FOLLOWING SYSTEM SOFTWARE WAS USED:

PACK	- packs several words into one	PLTPGE	- start a new plotting page
UNPACK	- unpacks word into 1 character words	LABELA	- label axes
SHIFT	- shifts bits in a word	PLTAXS	- plot axes
UNIT	- checks status (EOF, parity error, ready)	PLTBEG	- begin plot routines
	of specified unit	PLTDTS	- plot data specified
READMS	- reads direct access block	PLTSCA	- set plotting scale
WRITMS	- write direct access block	PLTSM	- plot symbol
GPIRMS	- prepare for direct access reads/writes		

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APPENDIX B

SEEFAR ANALYST'S AIDS

B-1

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Appendix B1

Calculation of Critical Horizon Coordinates

In determining whether a target position is in-view or out-of-view the first step is to consider the effect of intervening terrain. This is done by finding where the observer-target line intersects the closest line of known horizon values (as illustrated in Figure B1-1). This intersection location is referred to as (X, Y) . To find the horizon value, Z , at (X, Y) , one need only interpolate between the closest horizon values on the horizon scan, pictured as Z_1, Z_2 .

The problem of solving for X, Y , and Z breaks into eight cases (illustrated in Figure B1-2). These cases are determined by the relationship between the coordinates of the target and those of the observer.

Considering a pair of axes with origin at the observer position, each quadrant has been divided into two sectors. Targets in one sector have an observer-target line slope whose absolute value is less than or equal to one. In the other sector the absolute value of this slope is greater than one. The reason for this division will be explained by the following two examples.

Selecting quadrant 1, X , Y , and Z will be determined for the area where $XTGT \geq XOBS$, $YTGT \geq YOBS$ and $(XTGT - XOBS) \geq (YTGT - YOBS)$. (See Figure B1-3.)

Letting GRID be the grid of the map data $X = XTGT - GRID$, since the horizon is one scan away. Knowing X , we can solve for Y from the equation of the observer-target line:

$$Y = \frac{(YTGT - YOBS)}{(XTGT - XOBS)} (XTGT - XOBS - GRID) + YOBS.$$

It remains to solve for Z . Consider the target to be the $ITGT^{th}$ position on a scan and ZOLD to be an array containing old horizon values.

Let $DX = XTGT - XOBS$ and $DY = YTGT - YOBS$.

Then linearly interpolating,

$$Z = (1 - \frac{DY}{DX}) ZOLD (ITGT) + (\frac{DY}{DX}) ZOLD (ITGT-1)$$

Now consider a target in the upper portion of quadrant 1, where $XTGT \geq XOBS$, $YTGT \geq YOBS$ and $(XTGT - XOBS) < (YTGT - YOBS)$. See Figure B1-4.) In this example the closest line of known horizon values is formed by ZOLD (ITGT-1) and ZLATER (ITGT-1) rather than by two old horizon values. In this case

$$Y = YTGT - GRID$$

$$X = \frac{DX (DY - GRID)}{DY} + XOBS$$

$$Z = (1 - \frac{DX}{DY}) ZLATER (ITGT-1) + (\frac{DX}{DY}) ZOLD (ITGT-1)$$

Where DX , DY and $GRID$ are as defined in the previous example. Similarly, equations for X , Y , and Z may be derived for each of the eight sectors, as indicated in Figure B1-5.

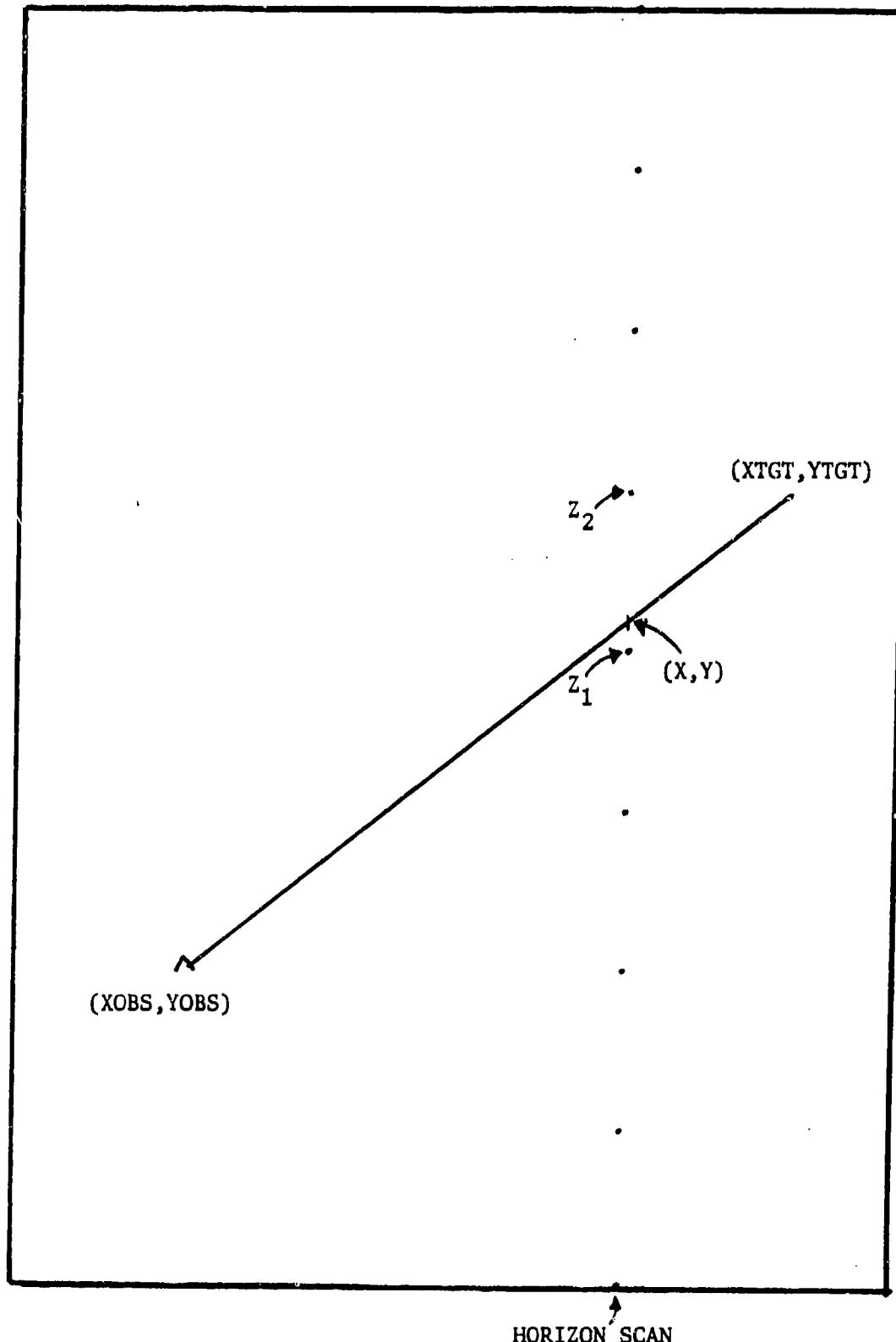


Figure B1-1
Locating Intersection of Observer - target line with
Closest Horizon Values

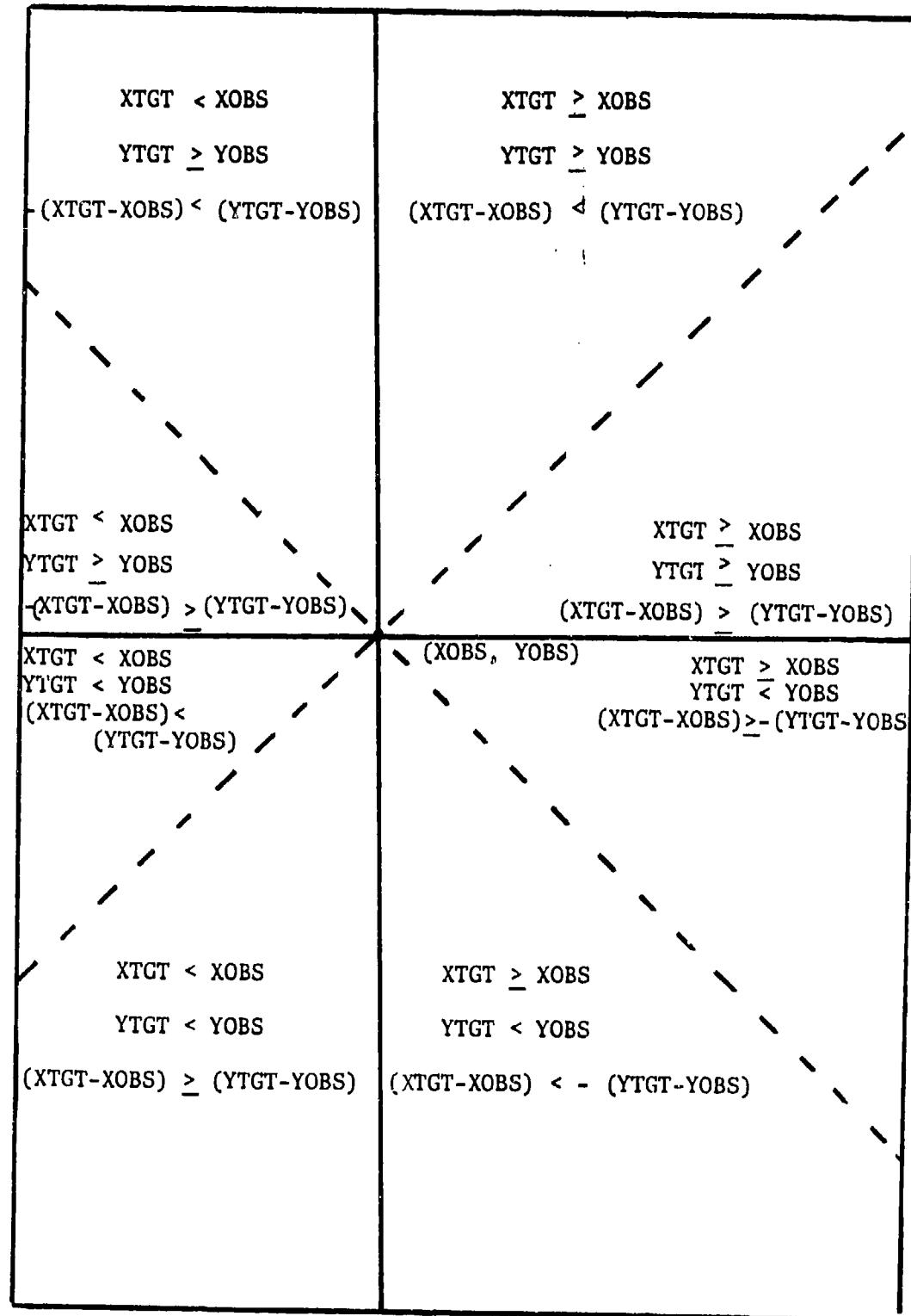


Figure B1-2
Eight Cases for Computing X,Y,Z

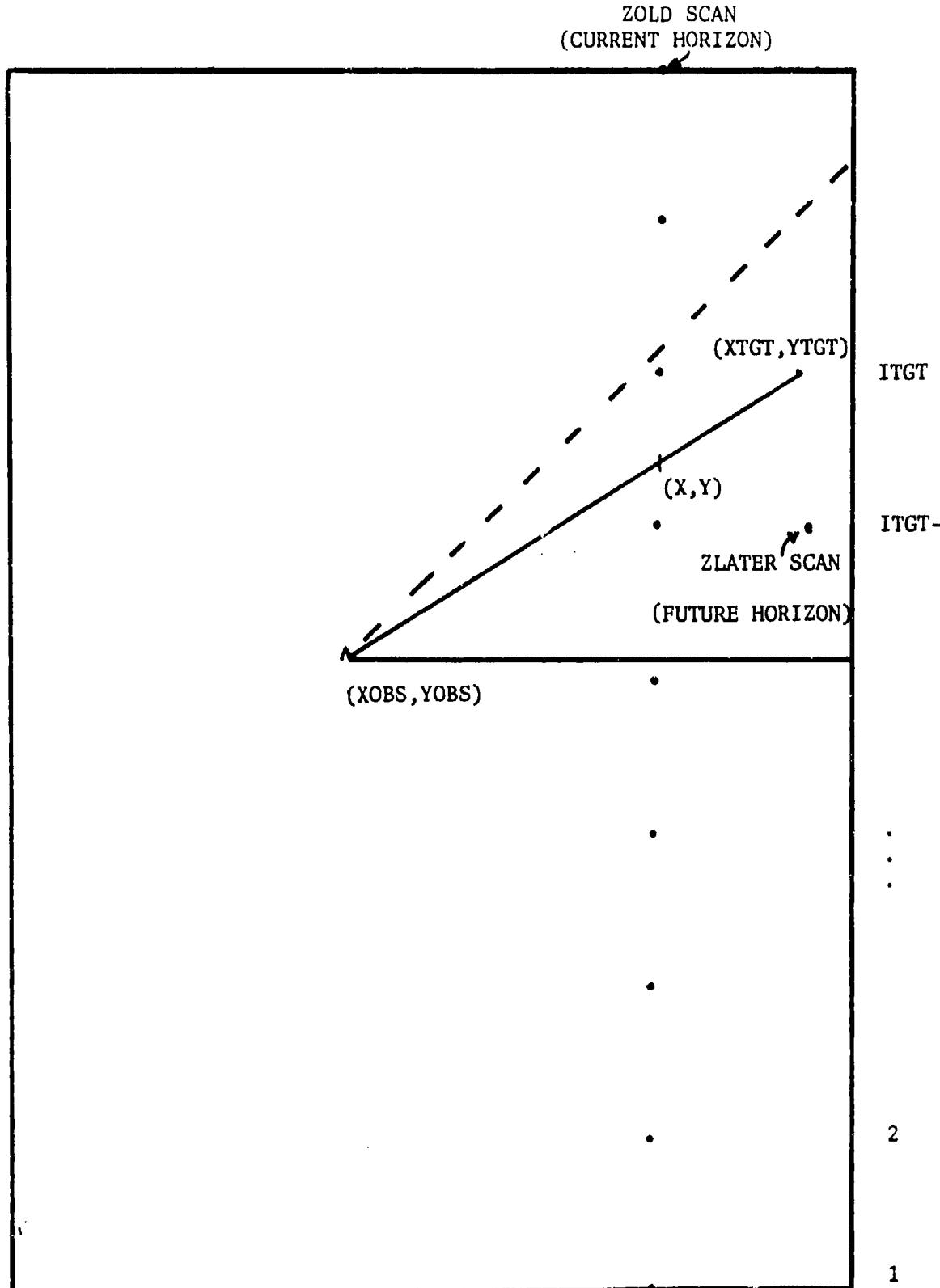


Figure B1-3

Solving for X, Y, Z when $XTGT \geq XOBS$, $YTGT \geq YOBS$ AND
 $(XTGT - XOBS) \geq (YTGT - YOBS)$

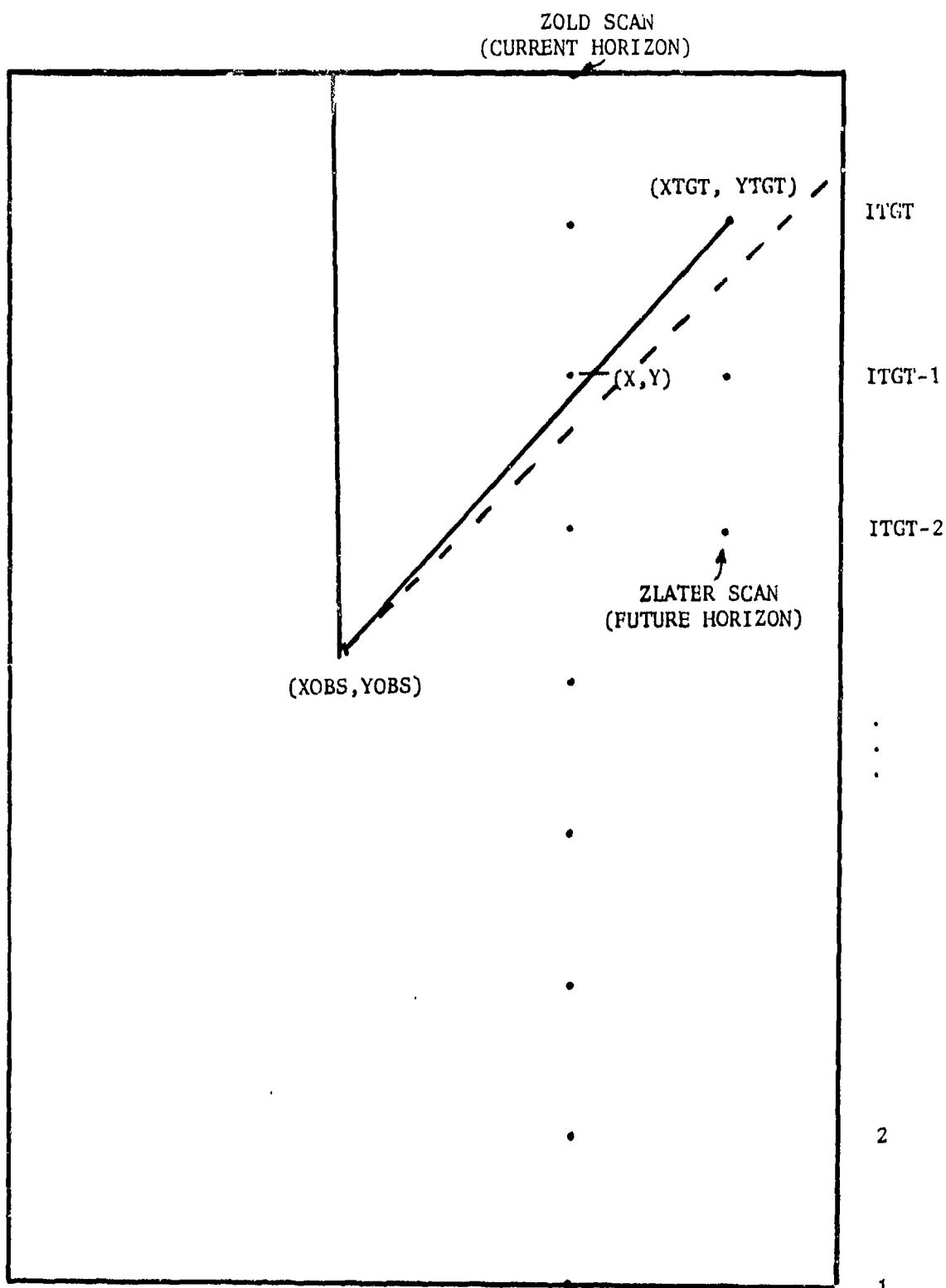


Figure B1-4

Solving for X, Y AND Z when $XTGT \geq XOBS$, $YTGT \geq YOBS$ and
 $XTGT - XOBS < (YTGT - YOBS)$

Figure B1-5
Equations for X, Y, Z for the ITGTth Target Position on a Scan (Eight Possible Cases)

Sector	X	Y	Z
1U DX>0 DY<0 DX<DY	$\frac{DX(DY-GRID)}{DY} + X_{OBS}$	YTGT-GRID	$(1 - \frac{DX}{DY}) ZLATER(ITGT-1)$ $+ (\frac{DX}{DY}) ZOLD(ITGT-1)$
1D DX>0 DY>0 DX>DY	XTGT-GRID	$\frac{DY(DX-GRID)}{DX} + Y_{OBS}$	$(\frac{DY}{DX}) ZOLD(ITGT)$ $+ (\frac{DY}{DX}) ZOLD(ITGT-1)$
2U DX<0 DY>0 -DX>DY	$\frac{DX(DY-GRID)}{DY} + X_{OBS}$	YTGT-GRID	$(1 + \frac{DX}{DY}) ZLATER(ITGT-1)$ $- (\frac{DX}{DY}) ZOLD(ITGT-1)$
2D DX<0 DY>0 -DX<DY	XTGT + GRID	$\frac{DY(DX+GRID)}{DX} + Y_{OBS}$	$(1 + \frac{DY}{DX}) ZOLD(ITGT)$ $- (\frac{DY}{DX}) ZOLD(ITGT-1)$
3U DX<0 DY<0 DX<DY	XTGT + GRID	$\frac{DY(DX+GRID)}{DX} + Y_{OBS}$	$(1 - \frac{DY}{DX}) ZOLD(ITGT)$ $+ (\frac{DY}{DX}) ZOLD(ITGT+1)$
3D DX<0 DY<0 DX>DY	$\frac{DX(DY+GRID)}{DY} + X_{OBS}$	YTGT + GRID	$(1 - \frac{DX}{DY}) ZLATER(ITGT+1)$ $+ (\frac{DX}{DY}) ZOLD(ITGT+1)$
4U DX>0 DY<0 DX>-DY	XTGT-GRID	$\frac{DY(DX-GRID)}{DX} + Y_{OBS}$	$(1 + \frac{DY}{DX}) ZOLD(ITGT)$ $- (\frac{DY}{DX}) ZOLD(ITGT+1)$
4D DX>0 DY<0 DX<-DY	$\frac{DX(DY+GRID)}{DY} + X_{OBS}$	YTGT + GRID	$(1 + \frac{DX}{DY}) ZLATER(ITGT+1)$ $- (\frac{DX}{DY}) ZOLD(ITGT+1)$

(XTGT, YTGT) = THE TARGET COORDINATES
 (X_{OBS}, Y_{OBS}) = THE OBSERVER COORDINATES
 GRID = MAP GRID
 DX = XTGT - X_{OBS}
 DY = YTGT - Y_{OBS}
 ZLATER = ARRAY HOLDING HORIZON REPRESENTING PREVIOUS ELEVATION
 ZLATER = FUTURE HORIZON VALUES CALCULATED FOR CURRENT SCAN

Appendix 82

In Appendix B1, a method was shown for calculation of x , y , and z , where (x, y) is the intersection of the observer-target line with the last running horizon line and z is the horizon elevation at the position (x, y) . This Appendix describes the method for projecting the horizon elevation to the target position. It is at this time that earth curvature is introduced into the line of sight calculations.

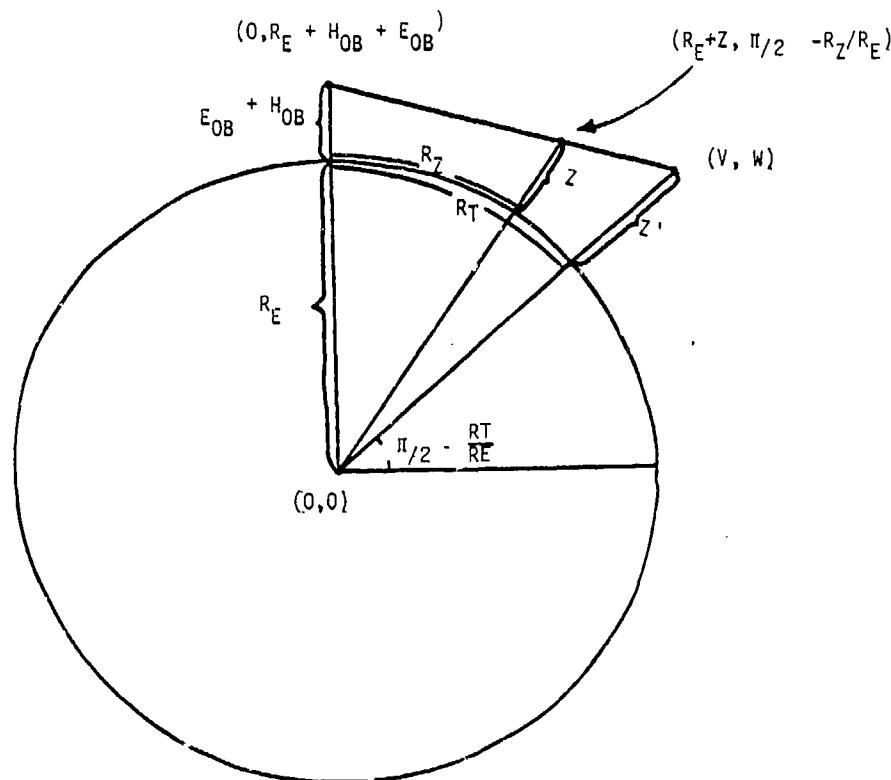
Letting R_E = the radius of the earth

E_{OB} = the elevation of the observer

H_{OB} = the height of the observer

R_Z = the range to the horizon line from the observer

and R_T = the range to the target from the observer
the situation might be drawn as follows:



Now

$$Z' = \sqrt{V^2 + W^2} - R_E$$

so if we can determine values V and W, we can find Z'.

But (V,W) is simply the intersection of lines $(0,0) - (V,W)$ and $(0, R_E + H_{OB} + E_{OB}) - (V, W)$.

The equation for $(0,0) - (V,W)$ is

$$Y' = AX' + B$$

where

$$B = 0$$

$$A = \tan(\pi/2 - (\frac{R_T}{R_E})) = \cot(\frac{R_T}{R_E})$$

And the equation for line $(0, R_E + H_{OB} + E_{OB}) - (V, W)$ is

$$Y' = A'X' + B'$$

where

$$B' = R_E + H_{OB} + E_{OB}$$

and

$$A' = \frac{(R_E + Z) \cos(\frac{R_Z}{R_E}) - (R_E + H_{OB} + E_{OB})}{(R_E + Z) \sin(\frac{R_Z}{R_E})}$$

Solving these two line equations simultaneously, then, for V and W

$$V = \frac{B'}{\cot(\frac{R_T}{R_E}) - A'}$$

$$W = \frac{\cot(\frac{R_T}{R_E}) B'}{\cot(\frac{R_T}{R_E}) - A'}$$

with A' and B' as defined above.

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APPENDIX C

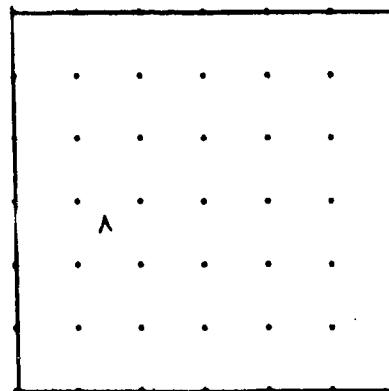
LOSMAP TIME COMPLEXITY

C-1

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APPENDIX C 1

The Time Complexity for an NXN Map Using the LOSMAP Algorithm



Consider a Map with N scan lines, and N points per scan line and an observer at a point such than n scan lines are to his "left" and m points on each scan are below him.

In example above, N = 7

$$n = 2$$

$$m = 3$$

If a calculation has to be made each time a profile crosses either a vertical or horizontal scan line, how many calculations have to be made to compute a LOSMAP?

There are N-n scan lines to the right of the observer. The first one (the one immediately to the observer's right) requires N crossings of vertical scan lines (one for each point on the scan); the second requires 2N crossings of vertical scan lines, etc. for a total number of crossings of

$$\begin{aligned} & N + 2N + 3N + \dots + (N-n) N \\ &= N \{1 + 2 + 3 + \dots + (N-n)\} \\ &= N \frac{(N-n)(N-n+1)}{2} \end{aligned}$$

There are n scan lines to the left of the observer.

The total number of crossings of these is

$$\begin{aligned} & N + 2N + \dots + n N \\ &= N (1+2+\dots+n) \\ &= N \frac{n(n+1)}{2} \end{aligned}$$

Therefore the total number of crossings of vertical scan lines is

$$\begin{aligned}n_v &= \frac{N}{2} \{(N-n)(N-n+1) + n(n+1)\} \\n_v &= \frac{N}{2} \{N^2 - nN + N - nN + n^2 - n + n^2 + n\} \\&= \frac{N}{2} \{N^2 + N + 2n^2 - 2nN\} \\&= \frac{N}{2} \{N^2 + N + 2n(n-N)\}\end{aligned}$$

Now $2n(n-N)$ is most negative when $n = N/2$,

Since $f(n) = 2n^2 - 2nN$

$$f'(n) = 4n - 2N$$

$$\text{Setting } 4n - 2N = 0, n = \frac{N}{2}$$

So $f(n)$ has its minimum or maximum at $N/2$

But $f''(N/2) = 4 > 0$ so $f(n)$ is minimal when $n = N/2$.

$$\begin{aligned}\text{So } n_v &\geq \frac{N}{2} \{N^2 + N + 2(\frac{N}{2})(-\frac{N}{2})\} \\&\geq \frac{N}{2} \{N^2/2 + N\} \\&> N^3/4 + N^2/2, \text{ order } N^3\end{aligned}$$

We have only looked at vertical scan lines. There are as many again crossings of horizontal scan lines, (similar analysis using m in place of n). This essentially doubles the number of calculations, but it still remains of order N^3 for a map with minimum crossings; that is, of order $\underline{N^3}$.

There are always less than $2N$ crossings (horizontal and vertical) for each of the N^2 target positions, so the order is $\underline{N^3}$.

Therefore the order is N^3 for the LOSMAP algorithm.

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